

# Miras and, in particular, R Leo

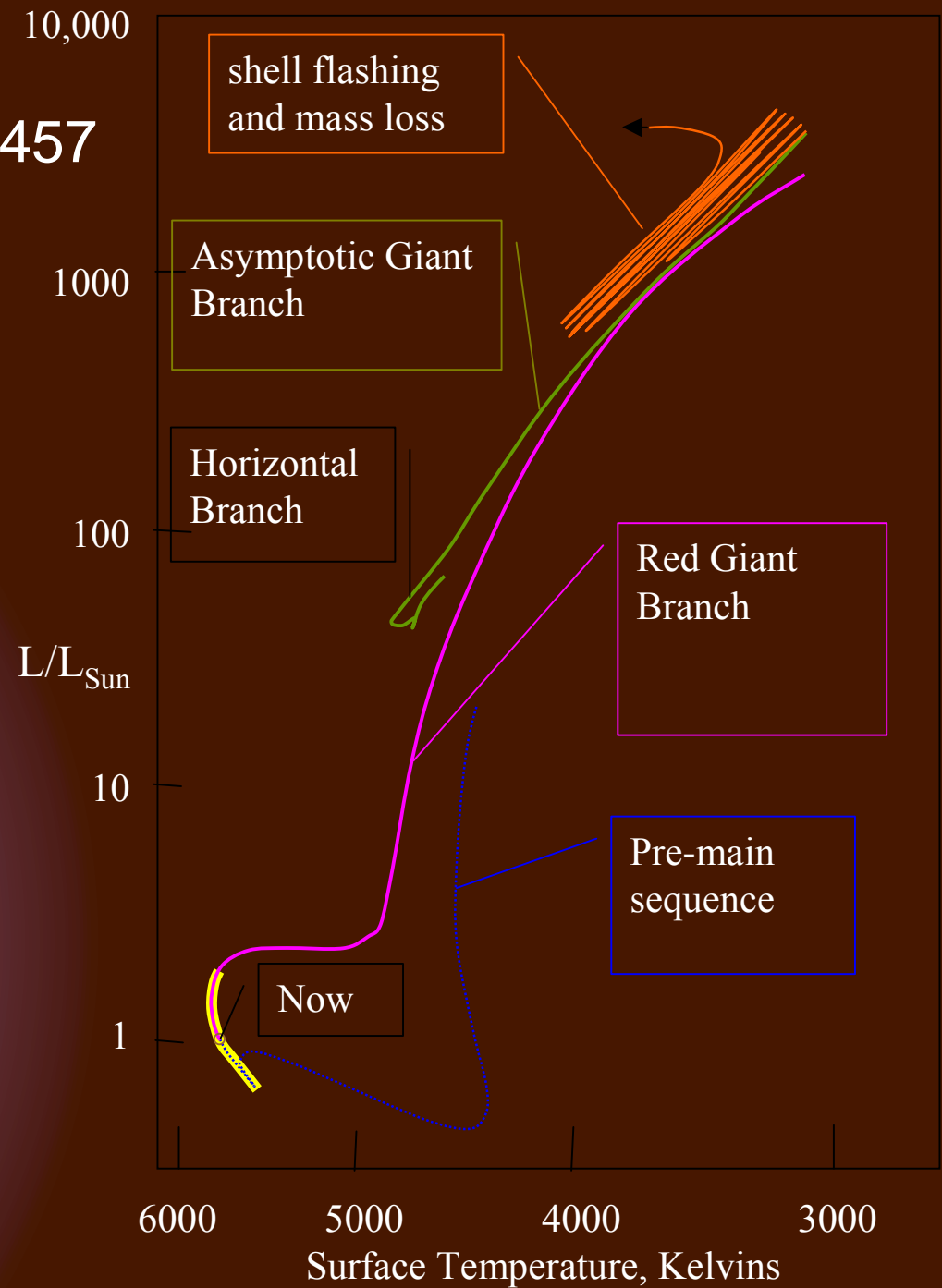
Results from  
theoretical calculations and  
observations



# Outline

1. Miras in context.
2. Atmospheric structure and time-dependence
3. Departures from spherical symmetry
4. How big are these stars, anyway?

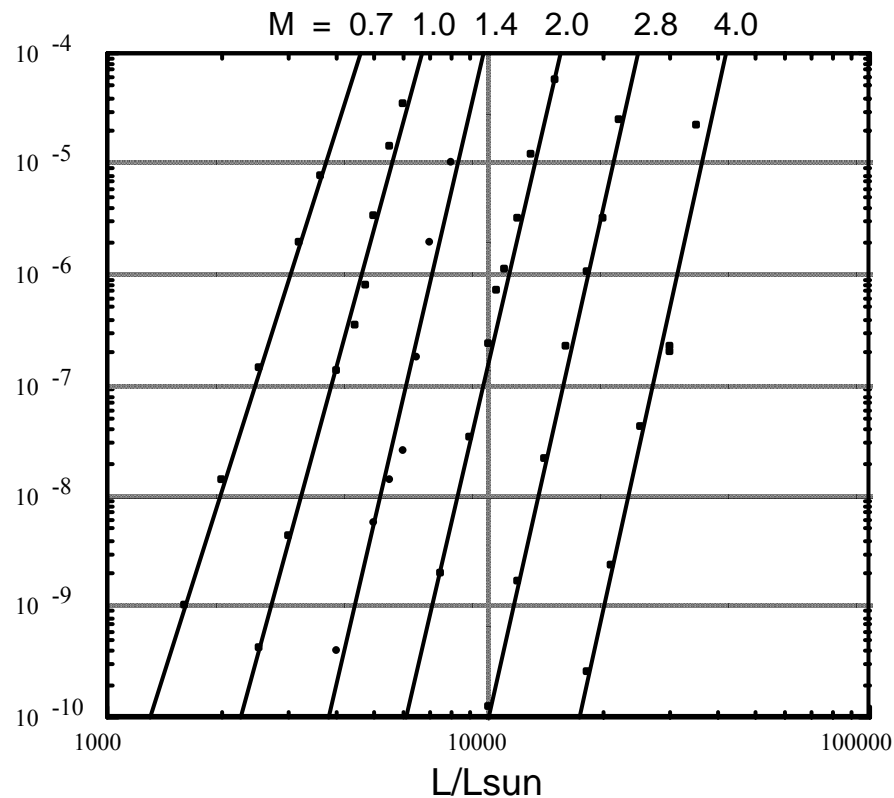
From Boothroyd, Sackmann,  
and Kramer 1993, Ap. J. 418, 457



# Terminal AGB mass loss

- Often treated using Reimers' Relation (proportional to  $LR/M$ )
- Detailed models give very different results
- Fates of low-mass stars ( $0.8-8 M_{\text{Sun}}$ ) depend on the mass loss law

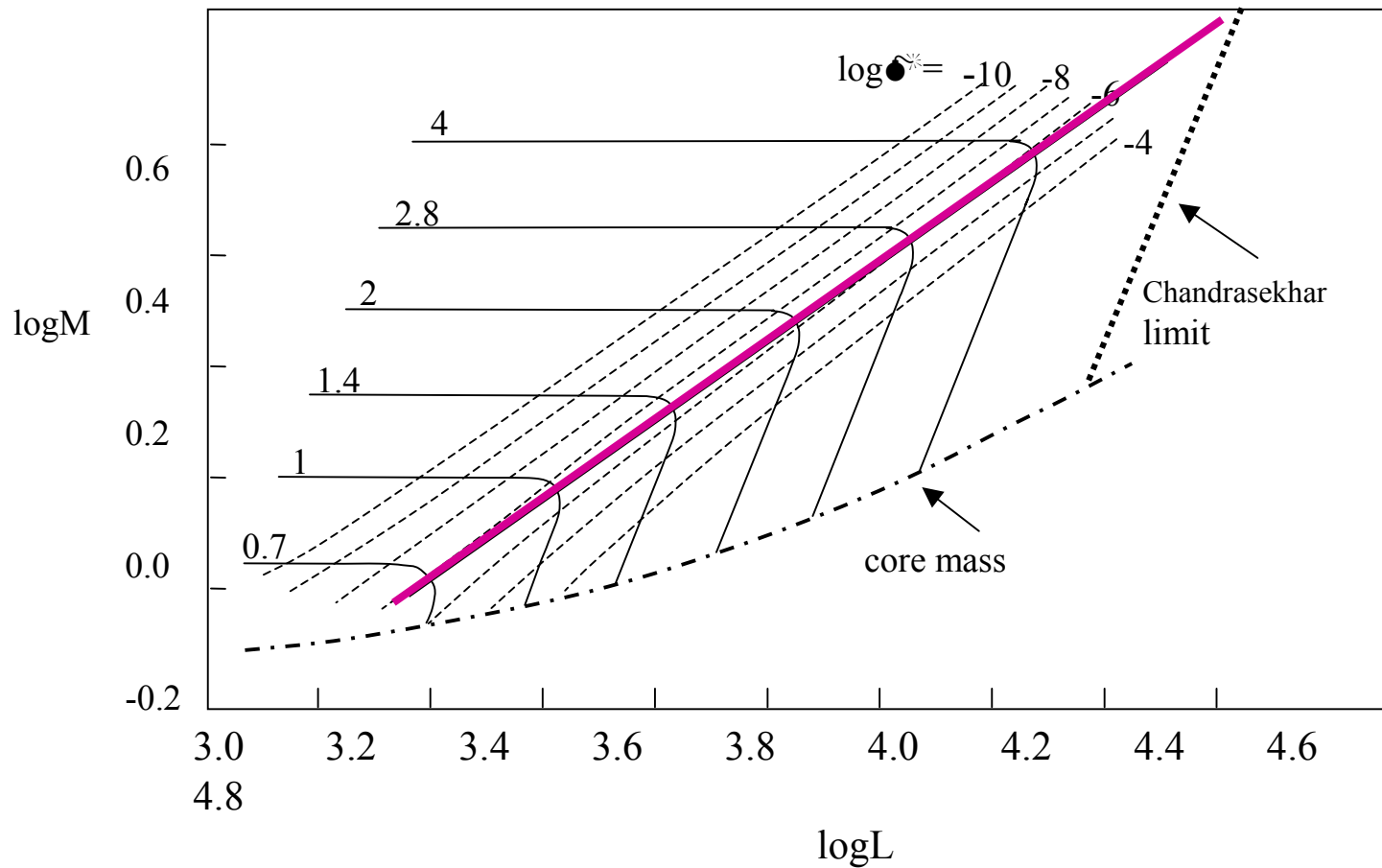
Models by Bowen (1995 grid) constraining evolution to follow reasonable tracks:



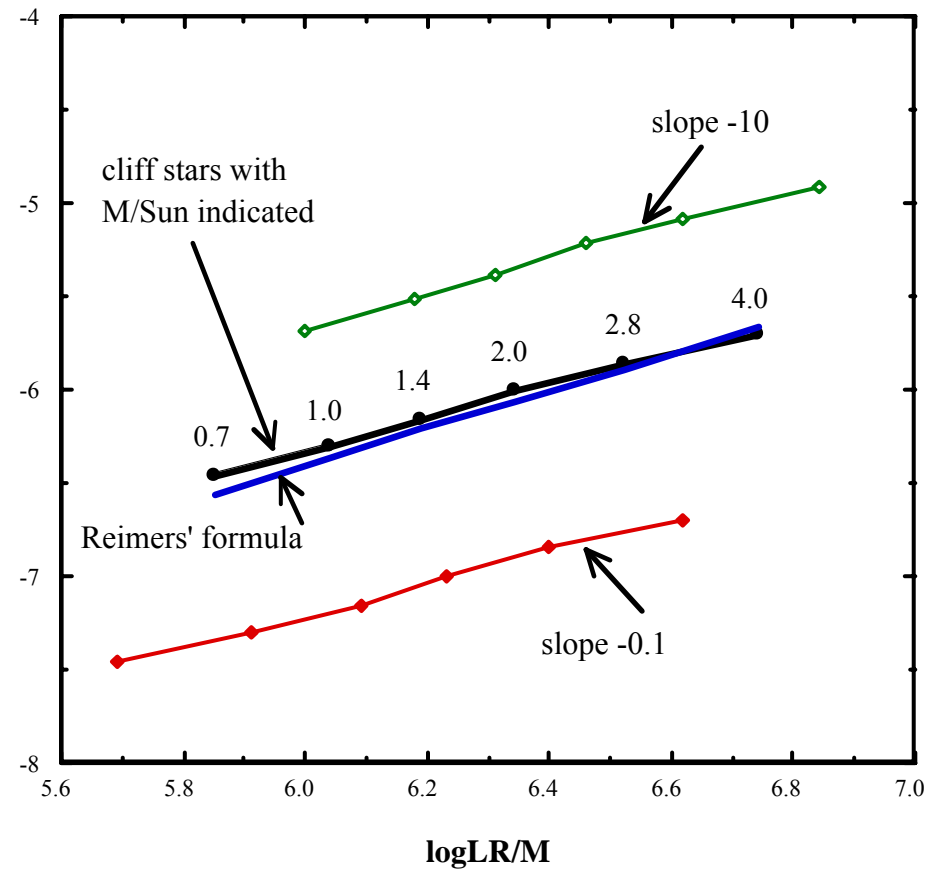
The dependence of mass loss rates on stellar parameters along the AGB is VERY steep.

Sources: see Willson 2000 In ARAA.

Stars evolving up the AGB lose little mass until they are close to “the cliff” where  $t_{\text{massloss}} \sim t_{\text{nuclear}}$ :

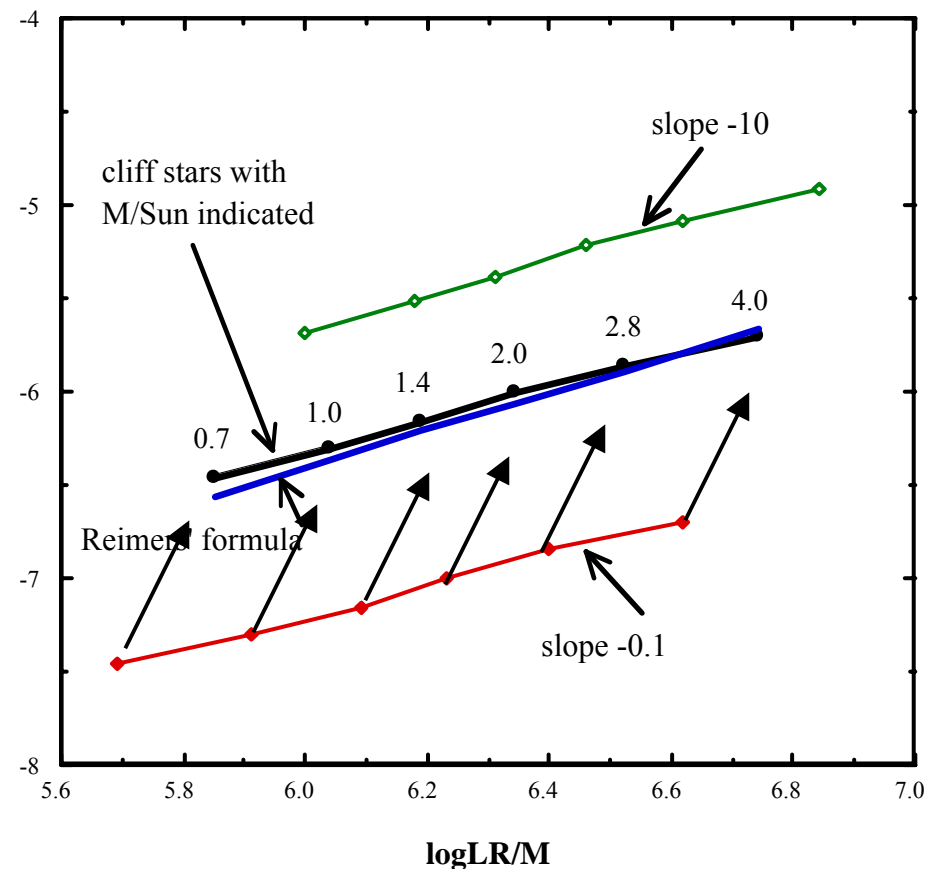


Empirical relations result from selection effects with very steep dependence of mass loss rates on stellar parameters.



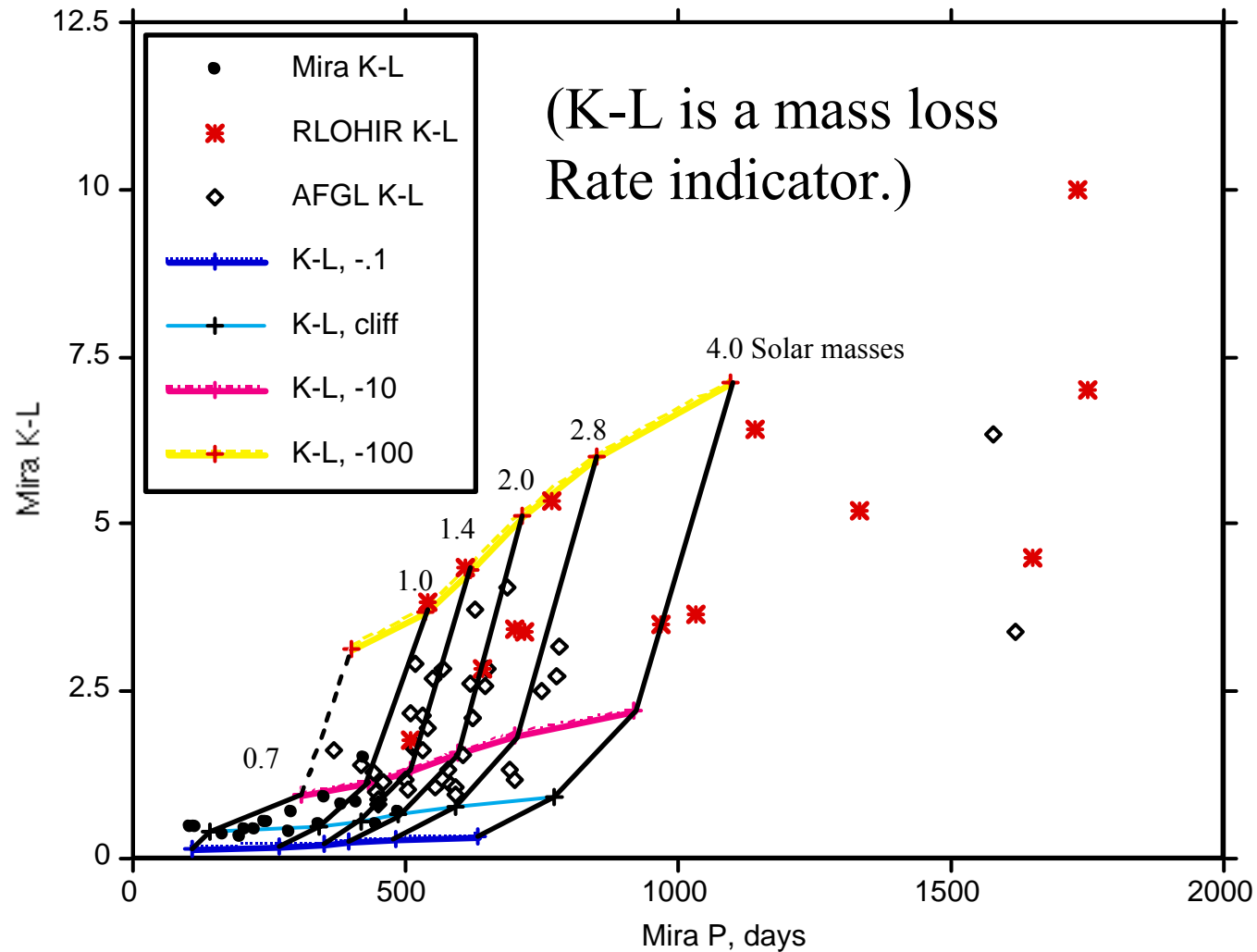
Individual stars do NOT follow Reimers' relation as they evolve.

Reimers' relation is a kind of main-sequence for mass loss: It tells us which stars are losing mass, not how one star will lose mass



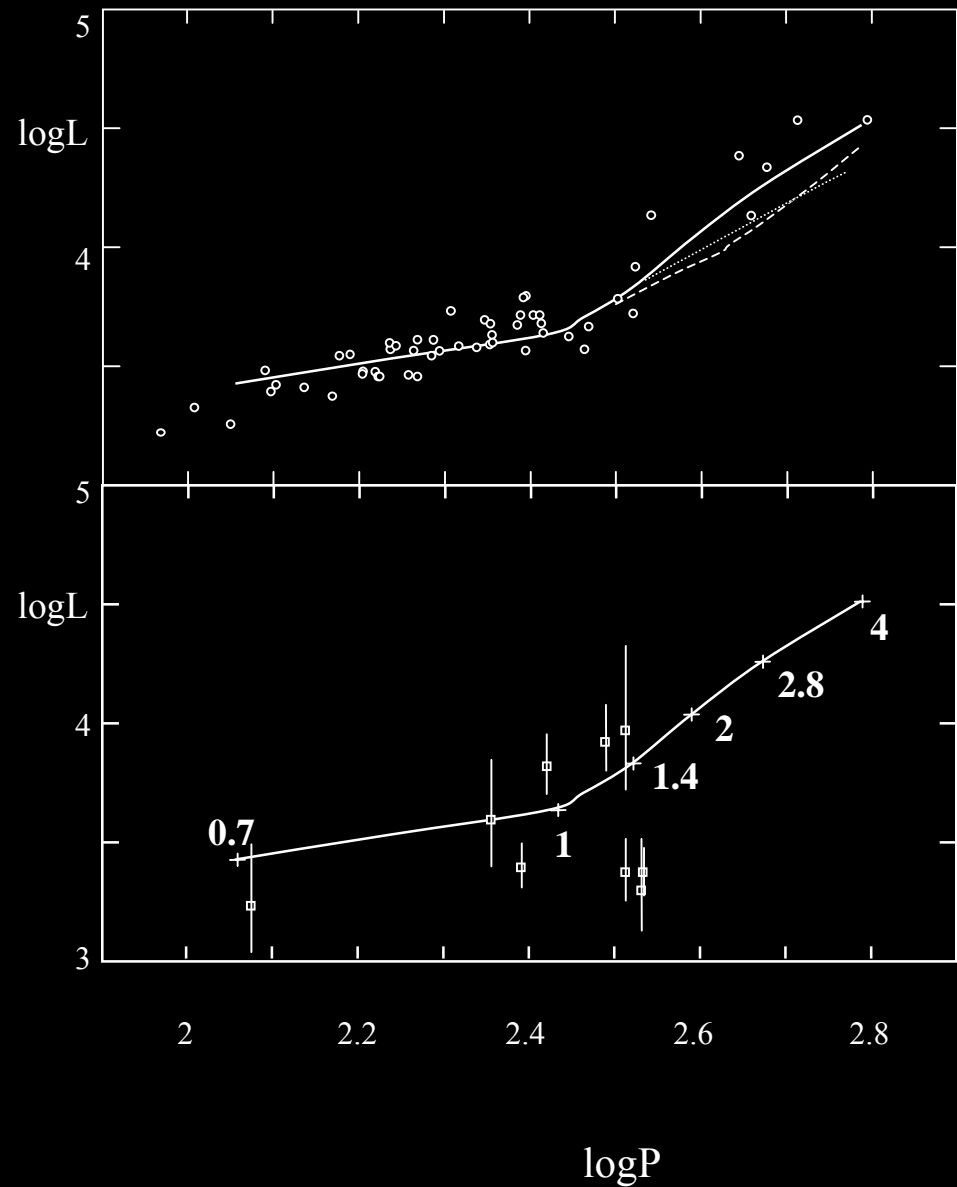


Observations of Miras and OH-IR stars confirm that Miras mark the location of the cliff:

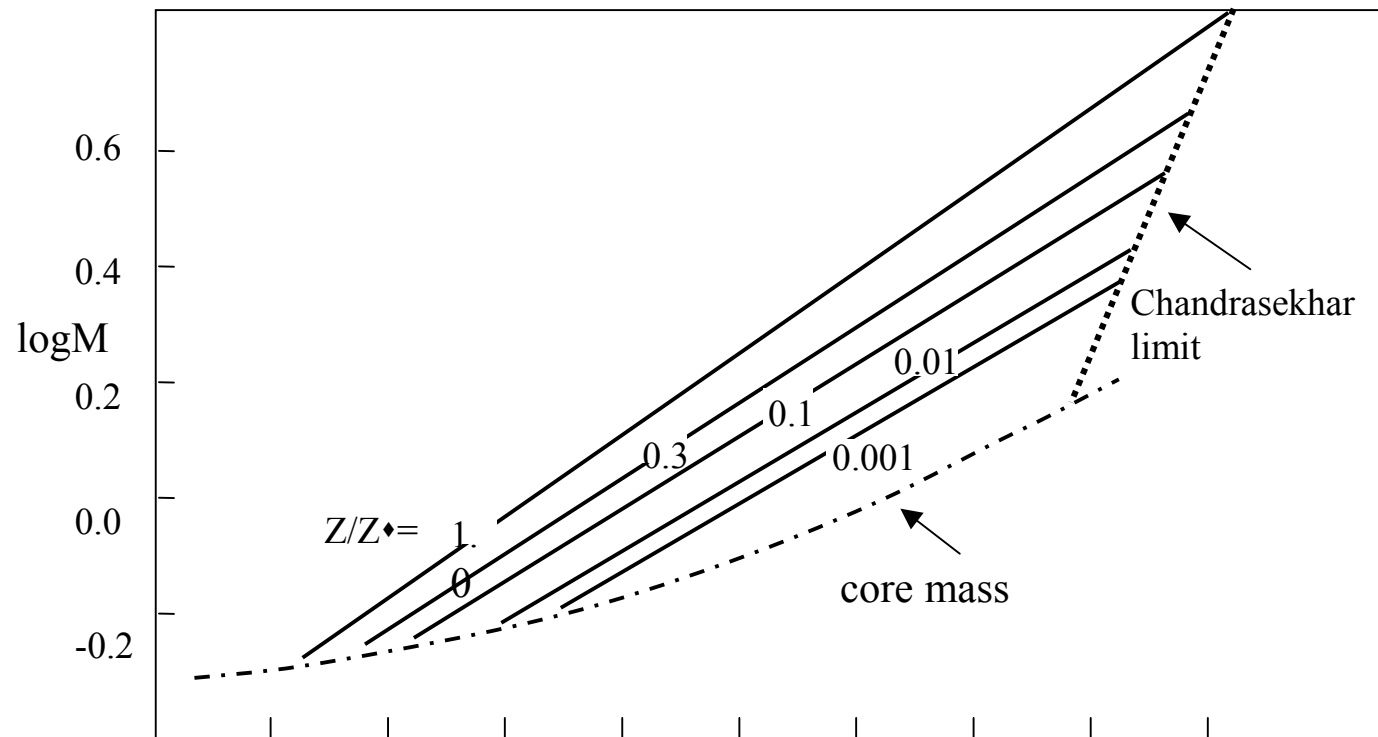



The cliff fits the  
observed Mira  
P-L relation from  
the LMC very well.

Hipparcos distances to  
Miras show a lot of  
scatter.



Now we can “predict” how different populations of stars will end:

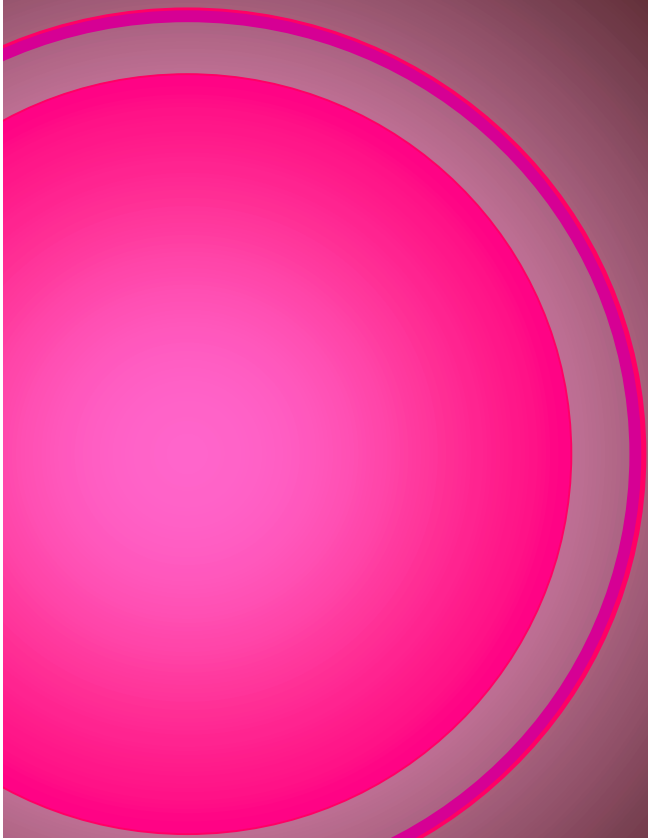


A decorative graphic on the left side of the slide consisting of two concentric circles. The inner circle is a bright magenta color, and the outer circle is a lighter, semi-transparent magenta. They are positioned on the left side of the slide, partially overlapping the dark brown background.

Evolutionary importance:

Miras signal the  
onset of the  
“superwind” that  
ends AGB  
evolution

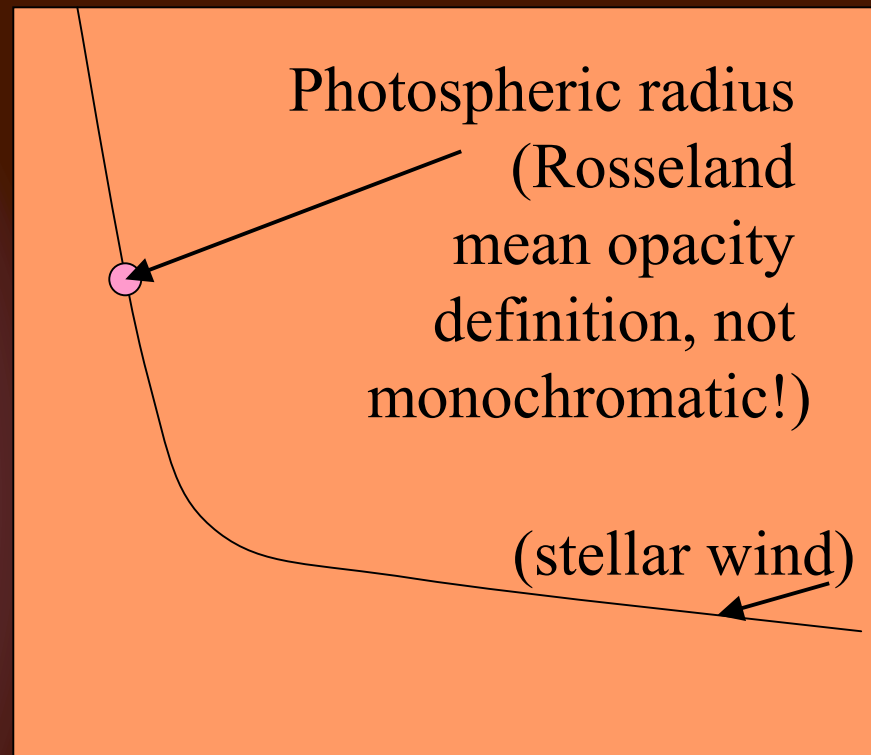
What would a Mira  
look like “up close”?



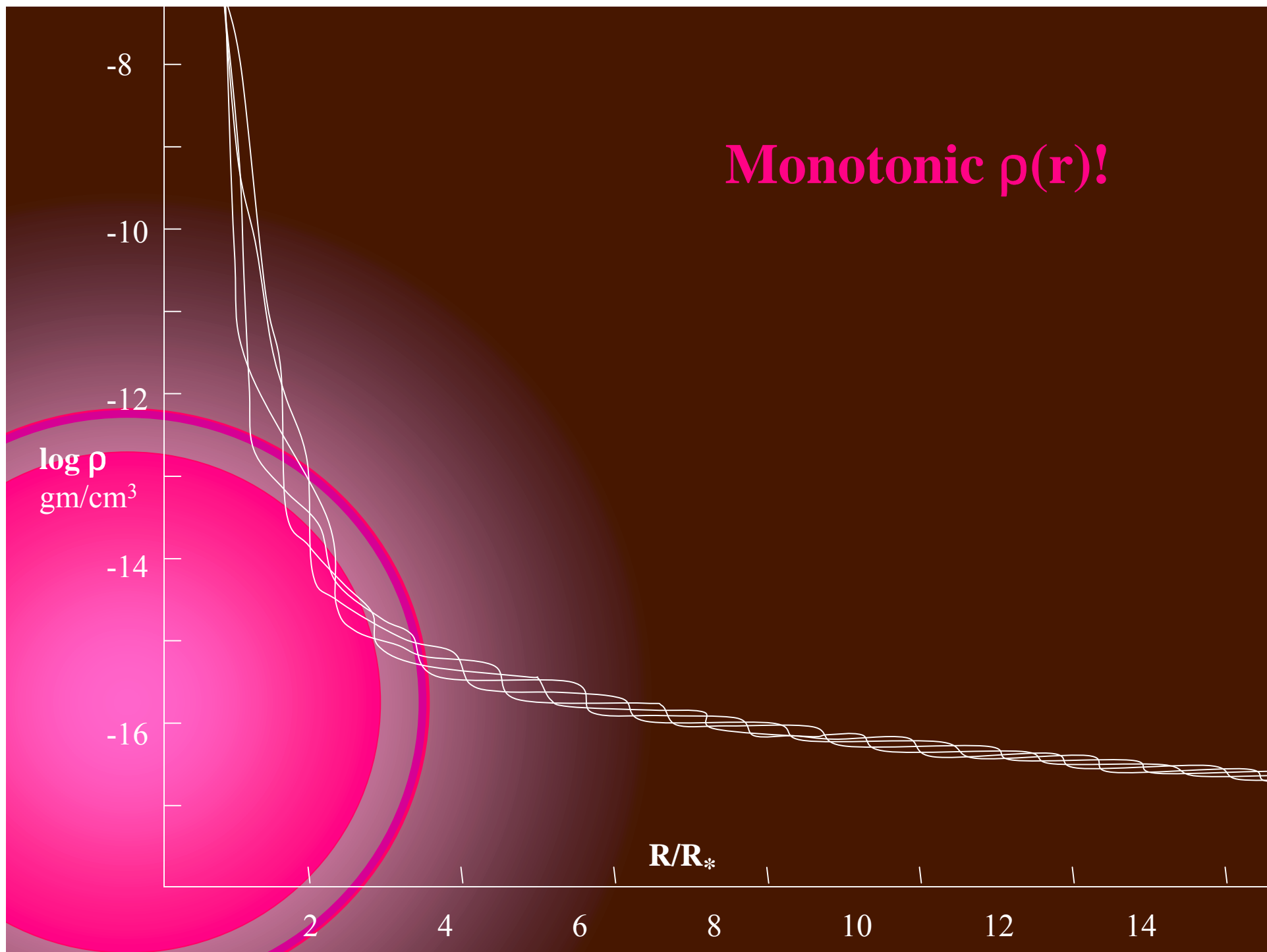
To first order, we should see an exponential decline in density merging into an inverse-square law decline



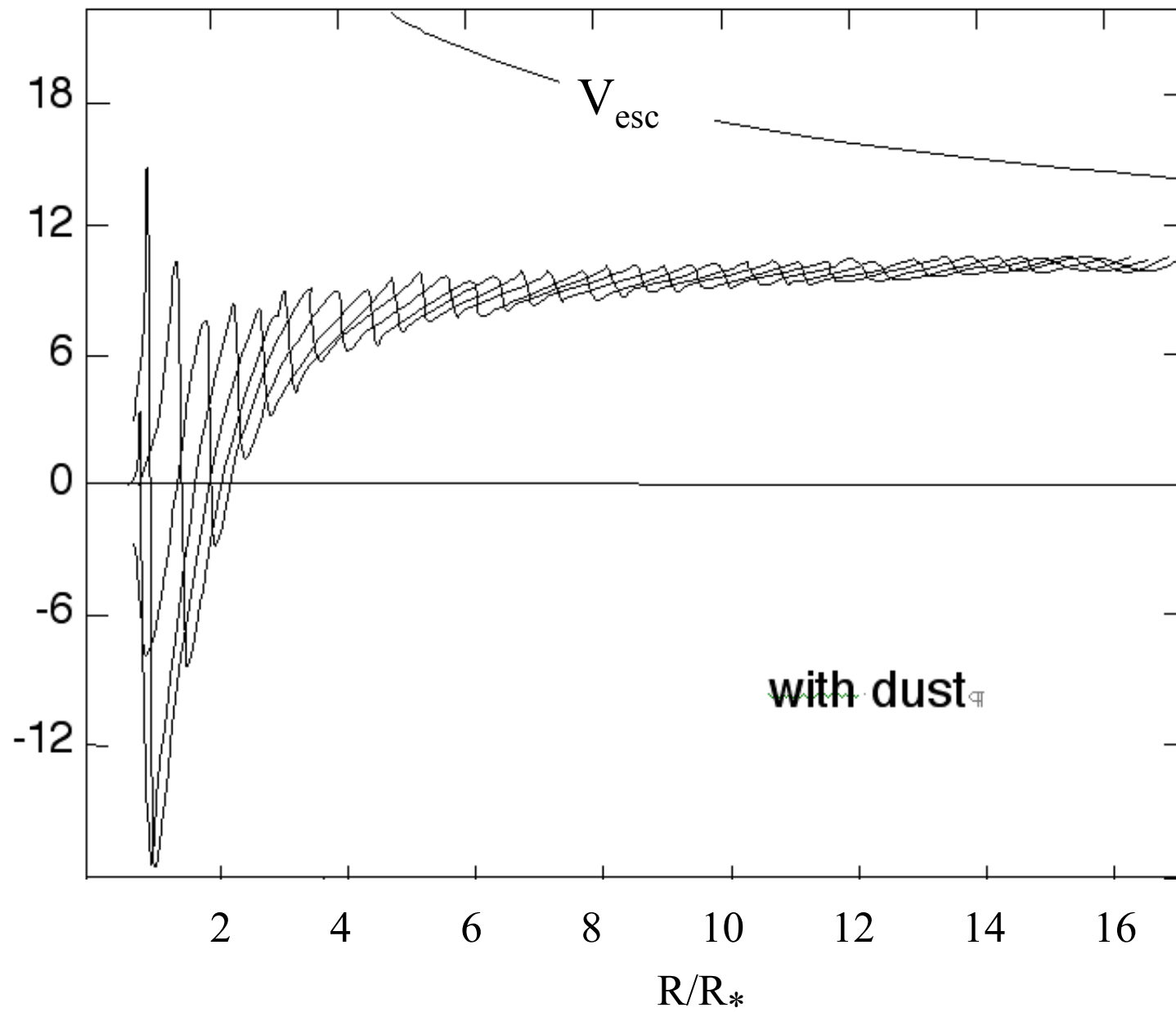
$\log \rho$



Radius->

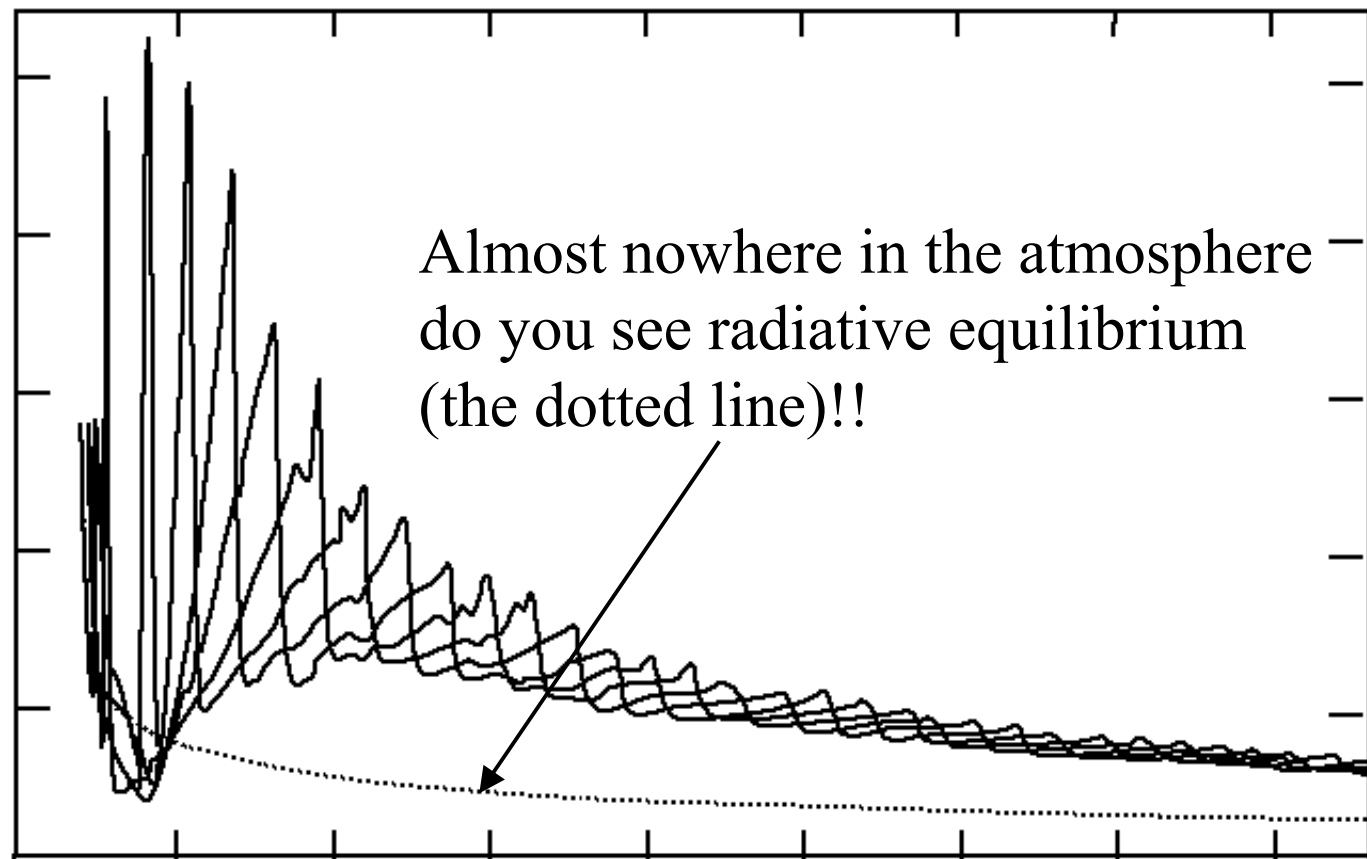


# Shocks form and propagate outward

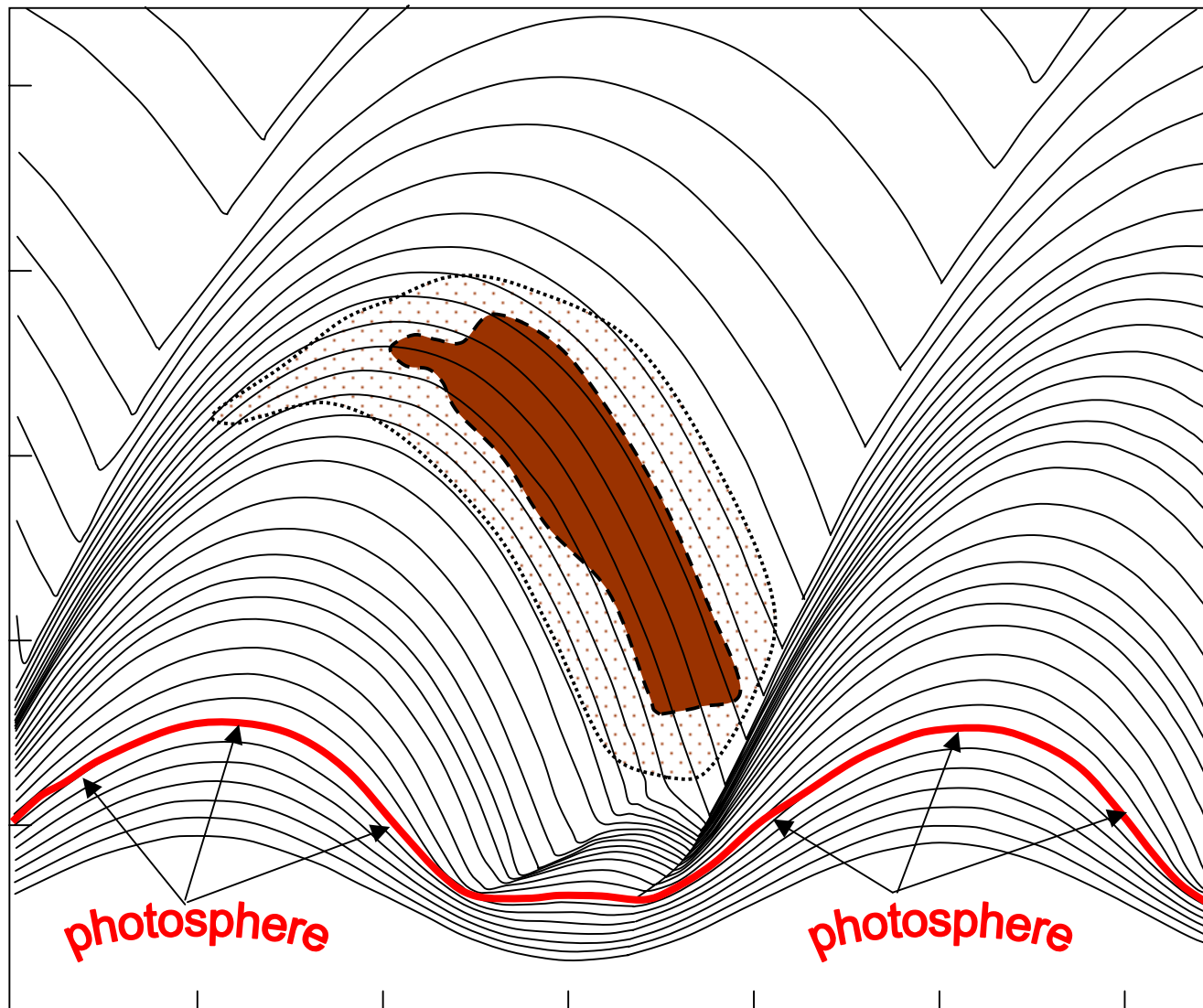




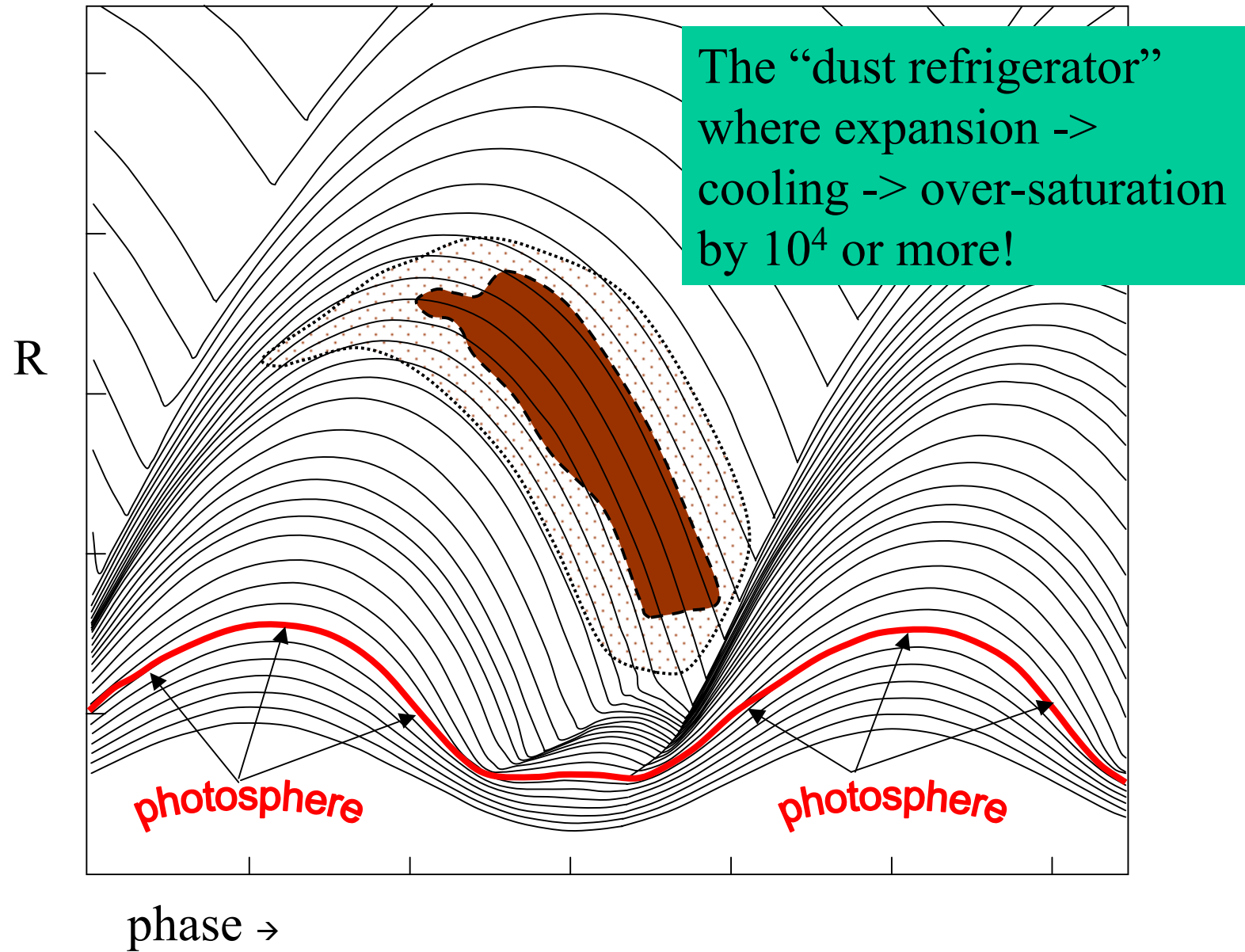
Shock compression  $\rightarrow$  heating  $\rightarrow$  radiative losses;  
expansion between shocks  $\rightarrow$  cooling and slower radiative gains.

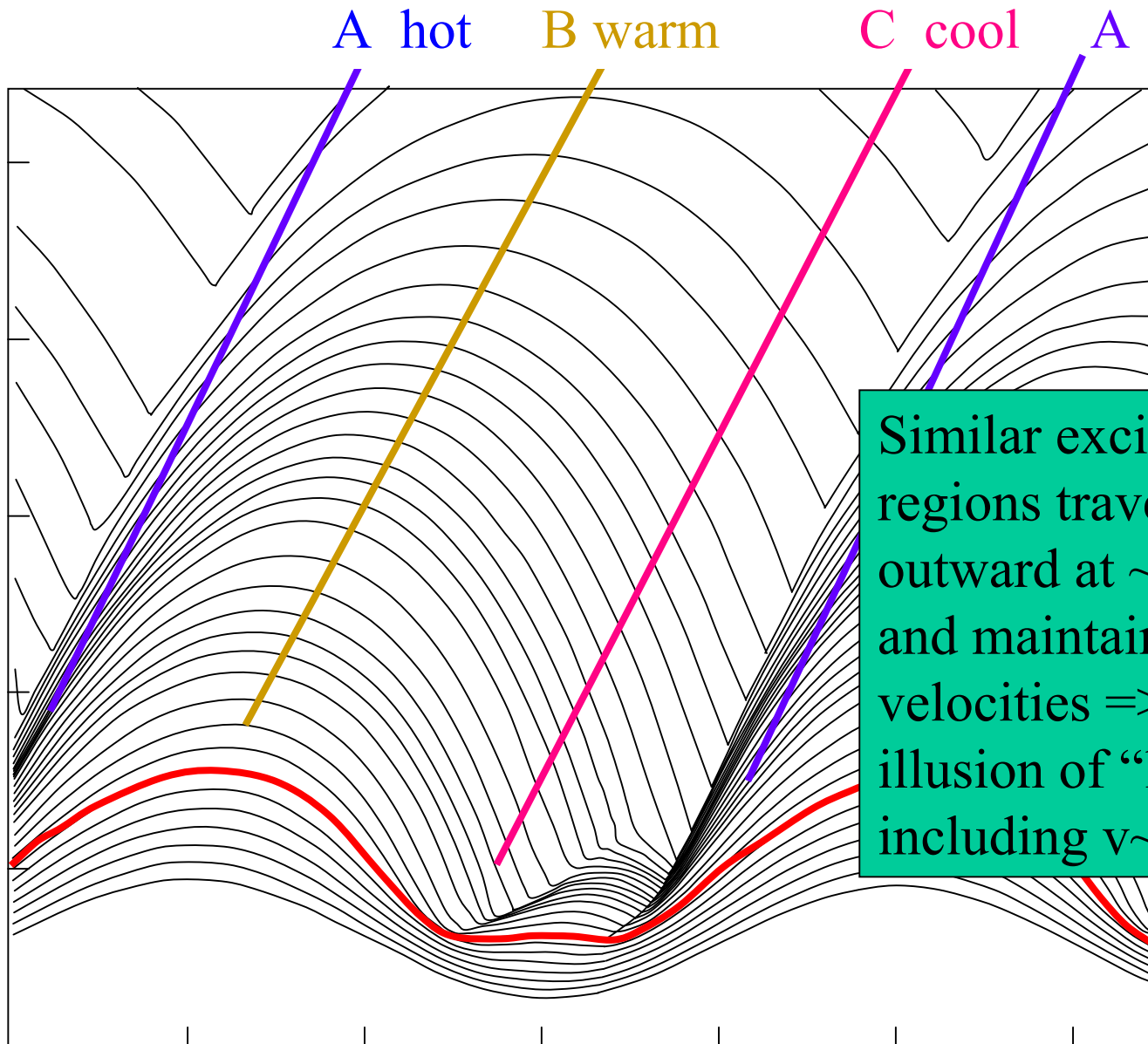


R



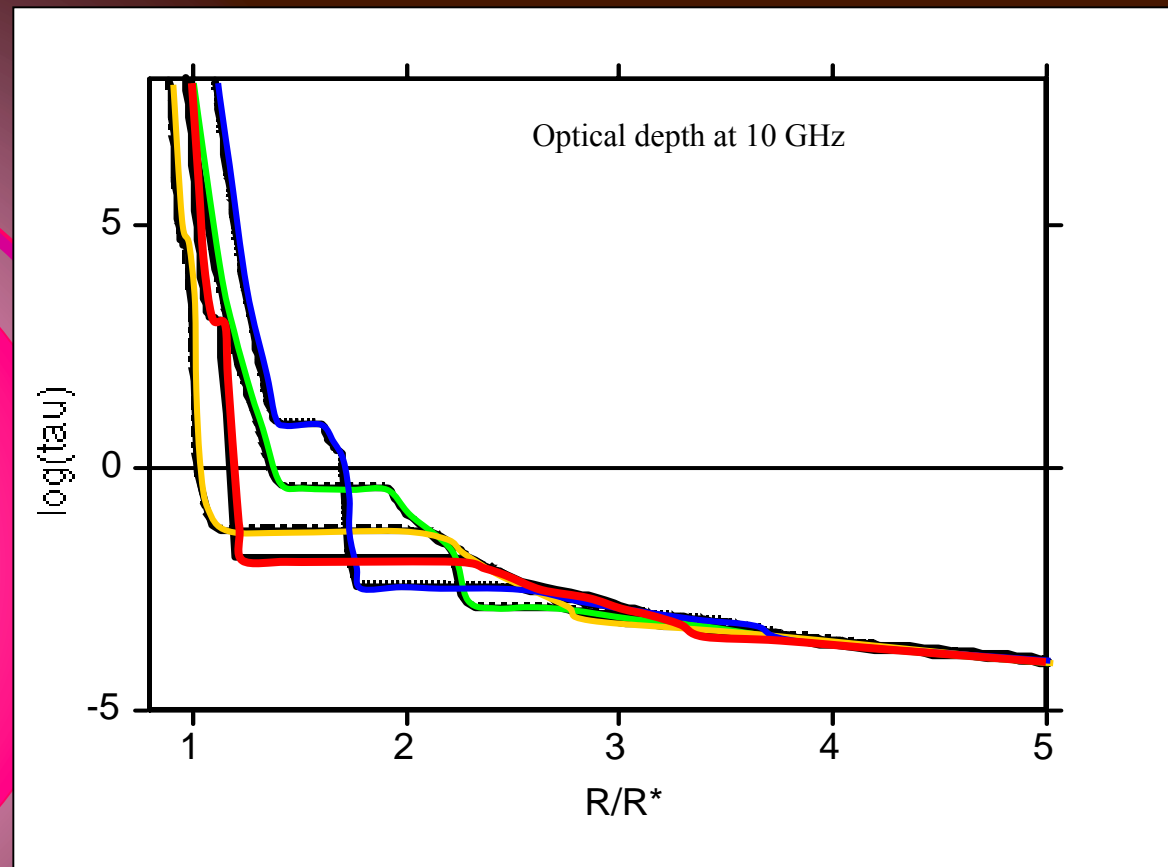
phase →



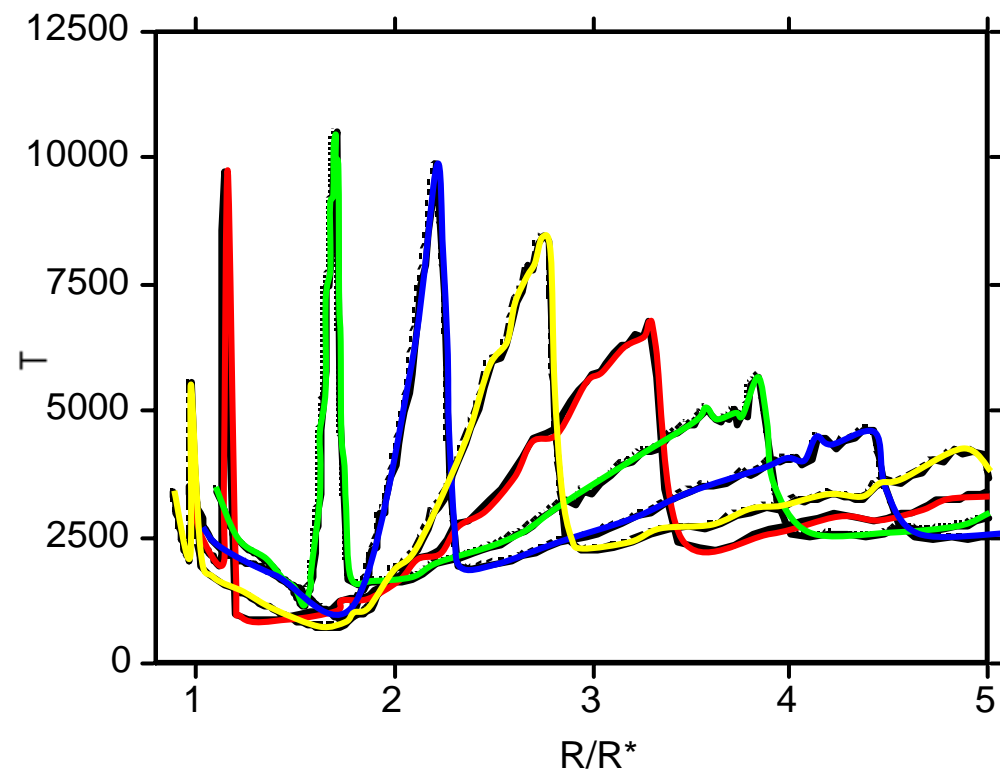


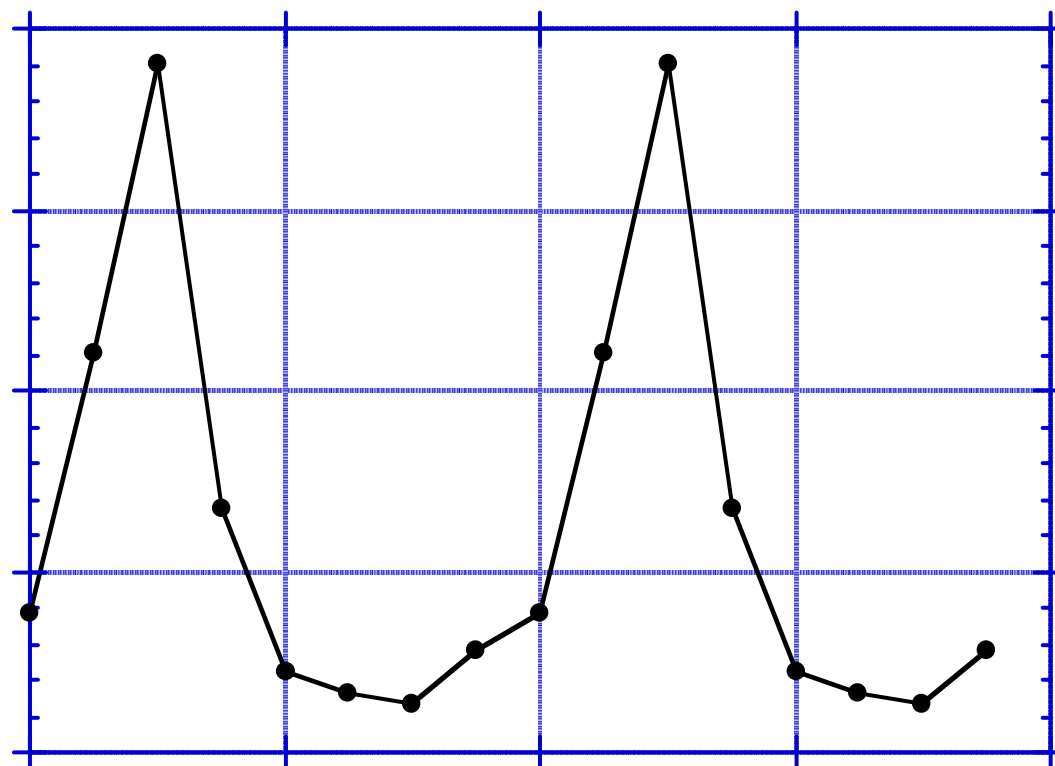
Similar excitation regions travel outward at  $\sim v_{\text{shock}}$  and maintain similar velocities  $\Rightarrow$  illusion of “layers” including  $v \sim 0$ .

In some parts of the spectrum, what you should see is an expanding shock front that becomes transparent at some phase, revealing the next rising shock front:




In these shocks,  $TR^2$  is nearly constant over most of the cycle





## Summary: The structure of the atmosphere

The density declines first steeply, then more slowly, monotonically, but with steps at the shocks.



The temperature rarely matches the radiative equilibrium temperature. Behind shocks,  $T$  rises to several thousand K; after expanding,  $T$  may be less than the radiative equilibrium temperature. This effect creates the “dust refrigerator” where super-saturation exceeds  $\times 10^4$

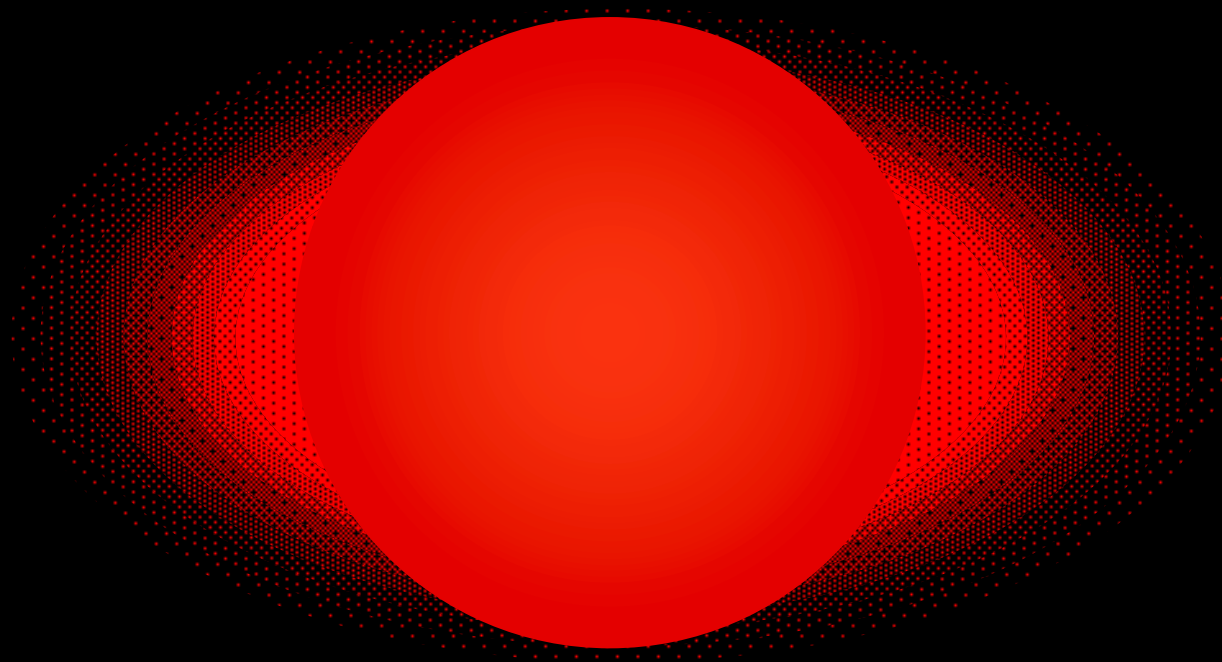
Large portions of the atmosphere are “falling in” at any given time.



What might cause departures from spherical symmetry?



Scattering in a circumstellar envelope leads to  
shape distortions when observed in polarized light



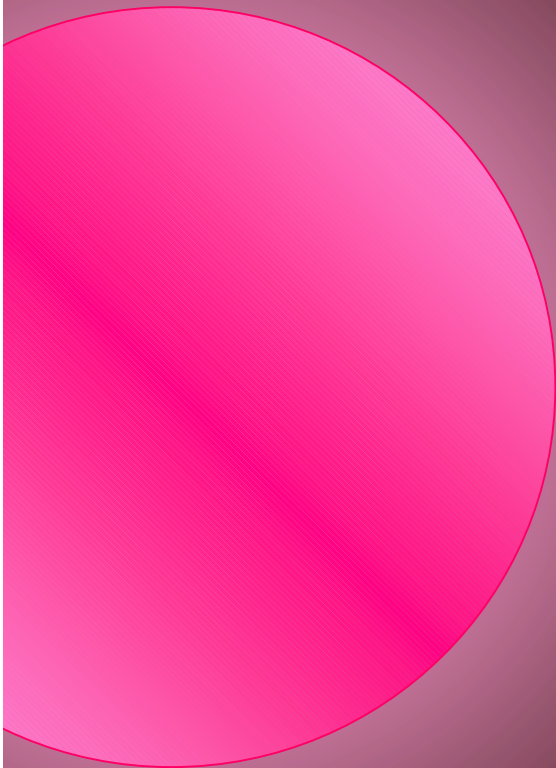
Atmospheric deviations from spherical symmetry may result from:

Non-radial pulsation

Magnetic field structures

Shock propagation  
instabilities

Large convective cells



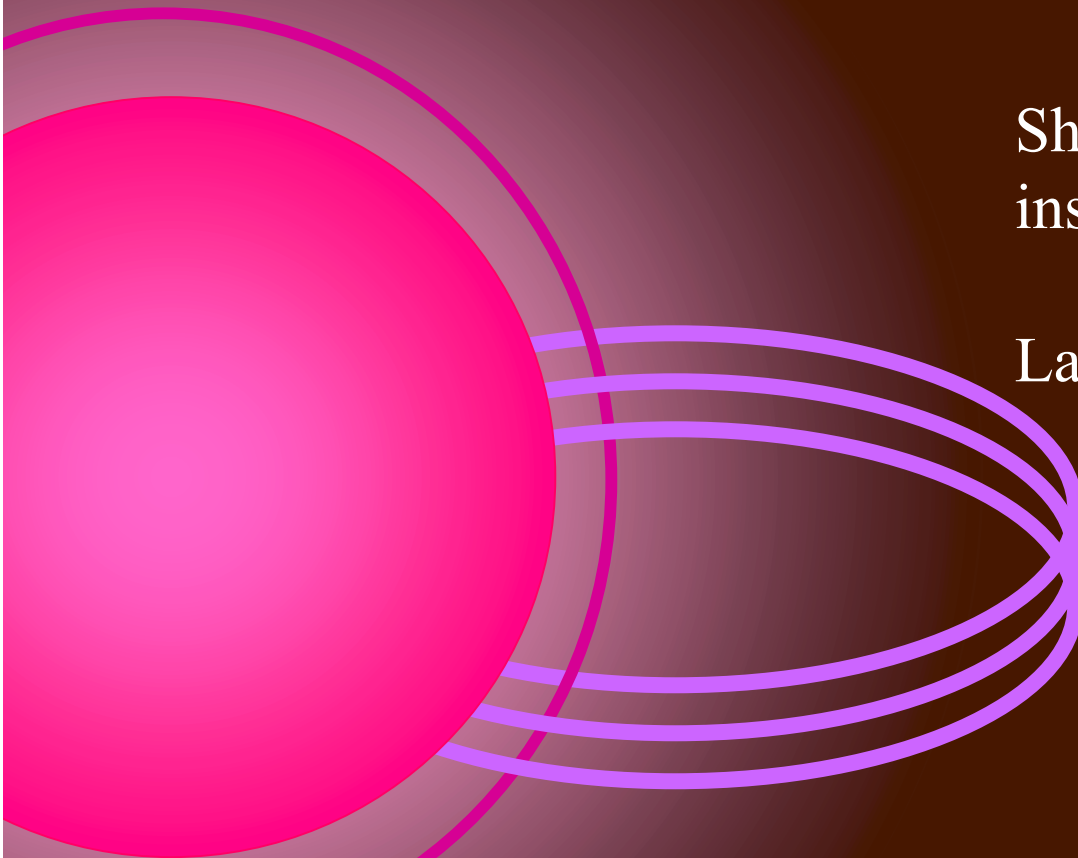
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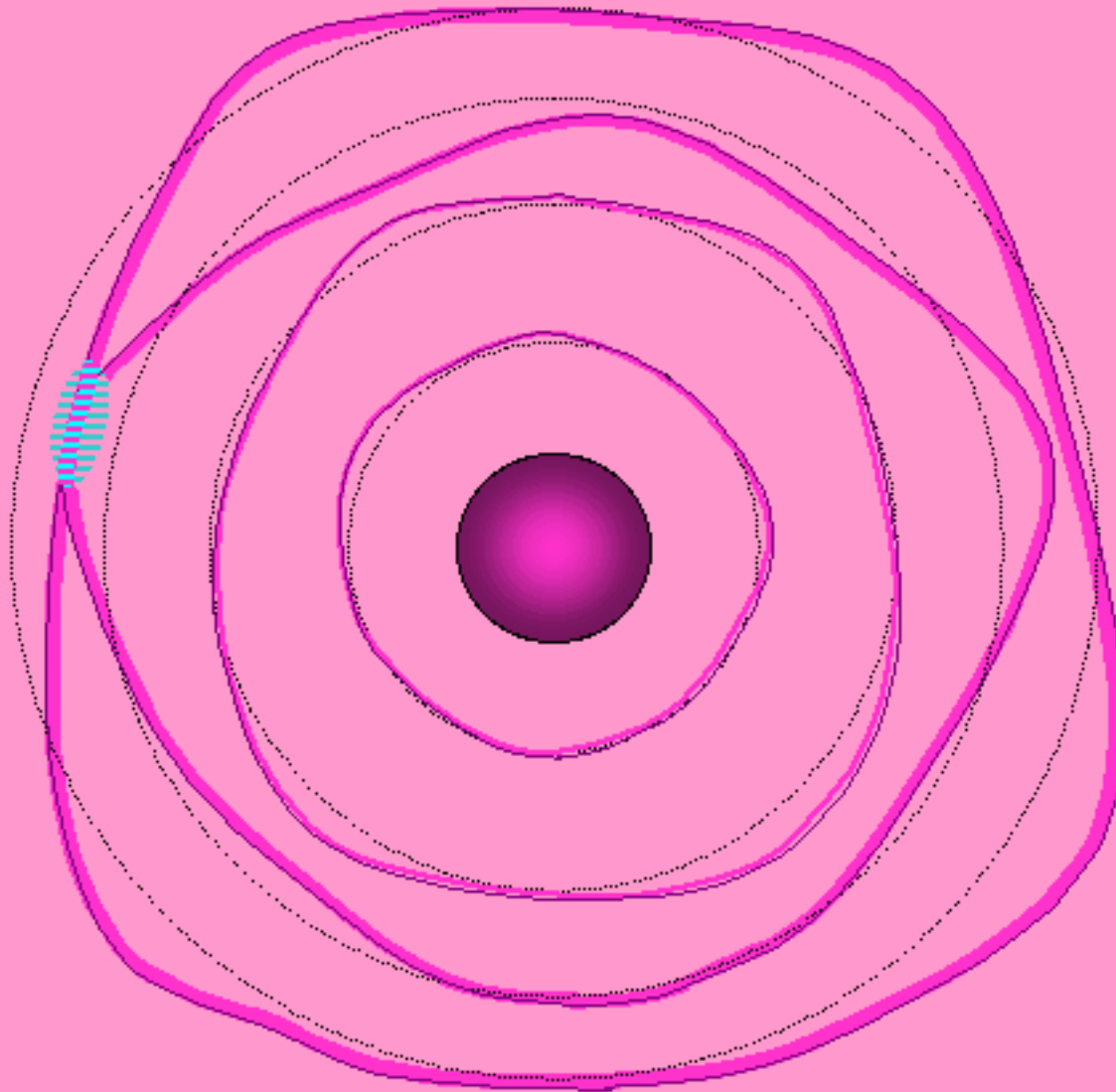
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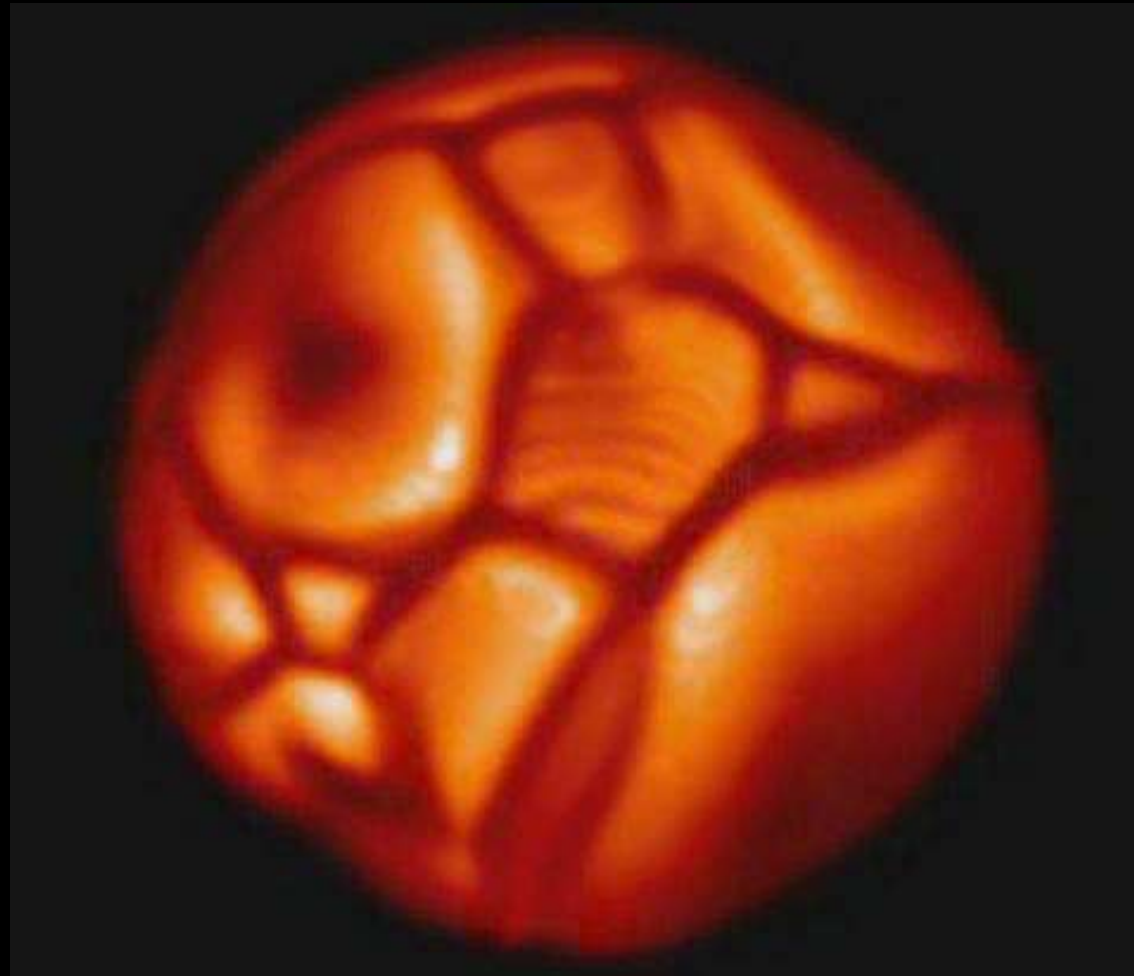
Large convective cells



Aperiodic shock propagation can lead to shocks “bunching up” and coalescing. Coalesced shocks will appear as bright spots.

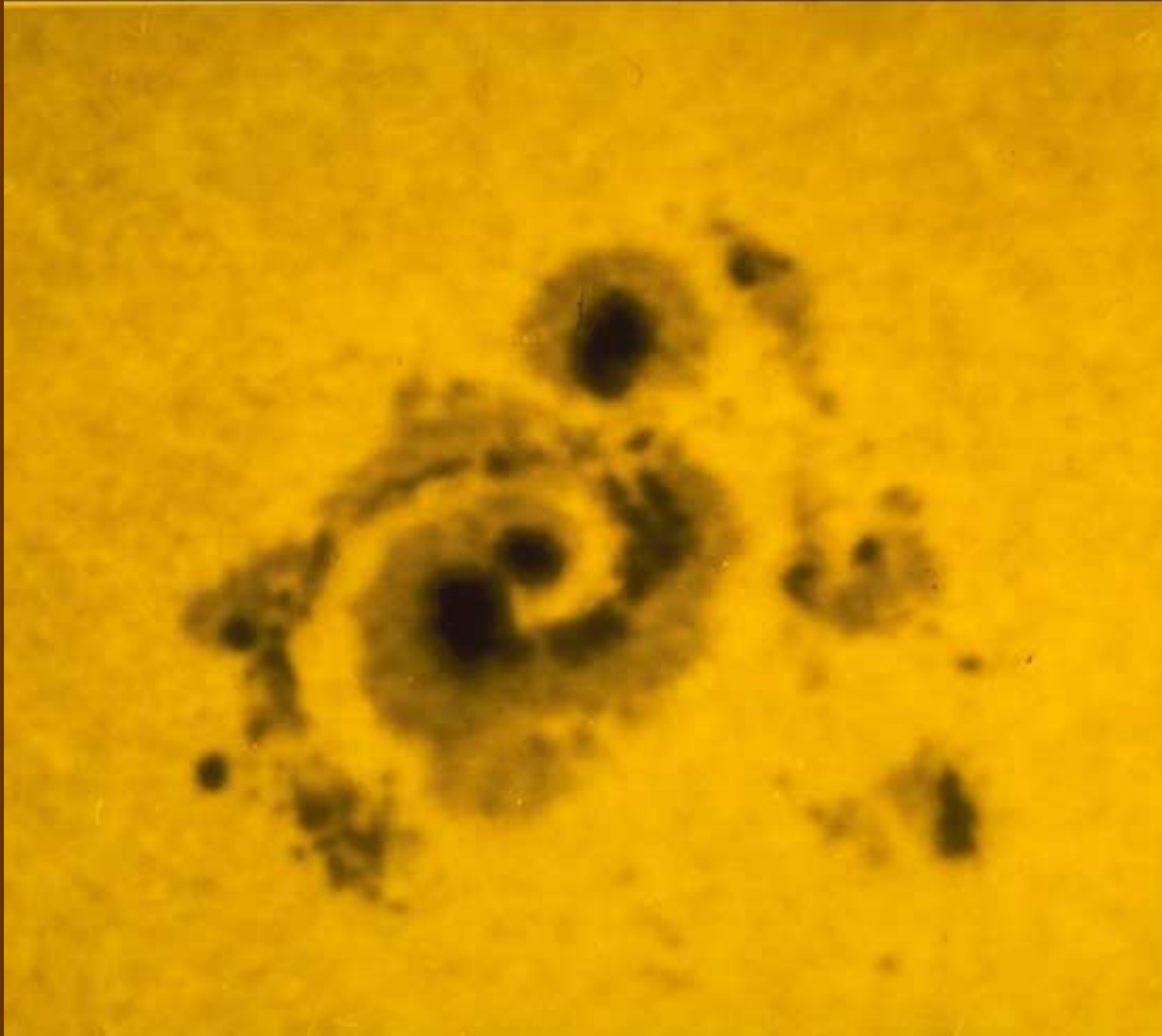


Simulations of convection in giant stars suggest that these could produce large, even bipolar, structures:



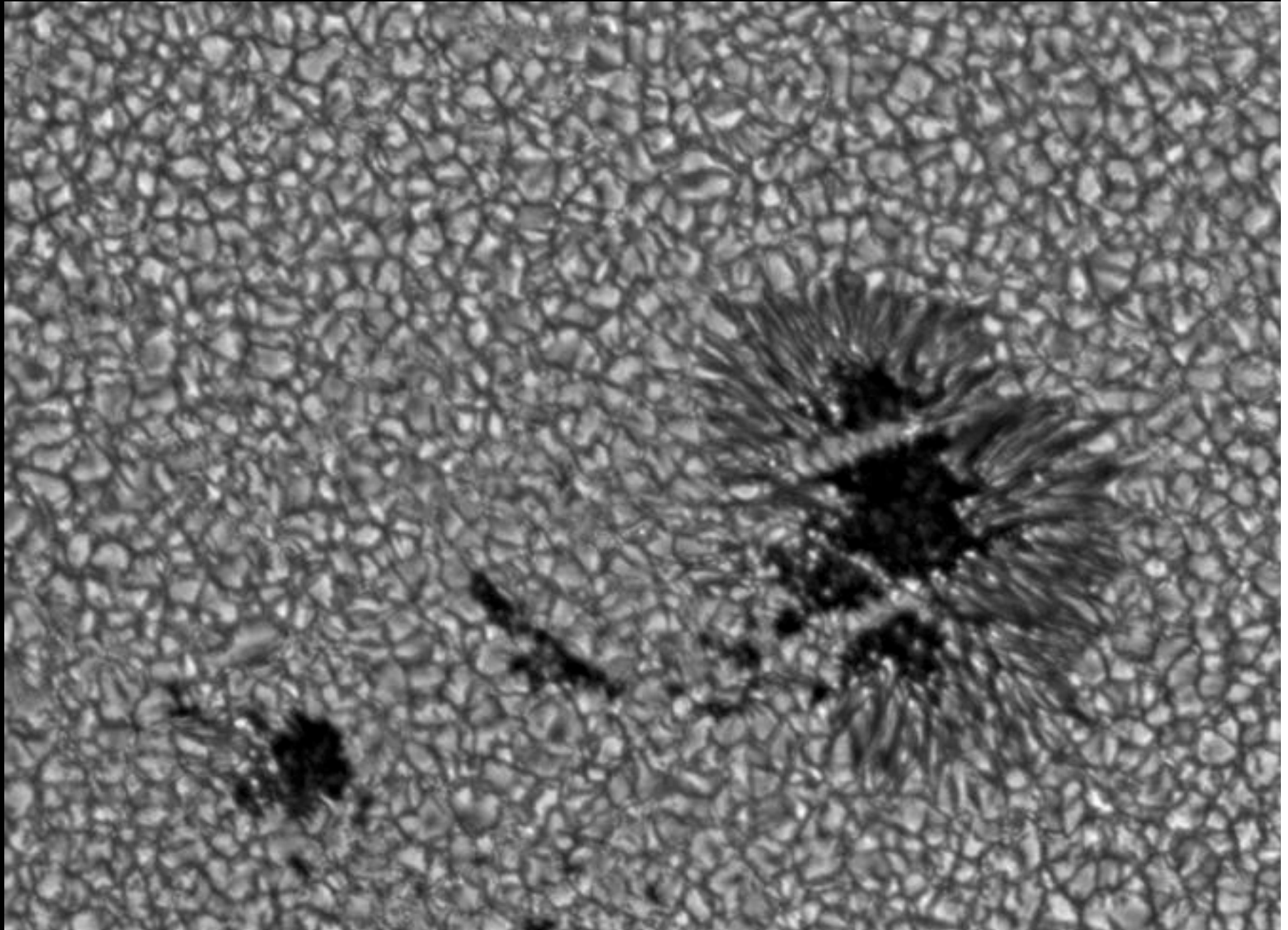
Freytag, 2000 - see <http://www.astro.uu.se/~bf/movie/movie.html>

Of course, starspots belong on the list:

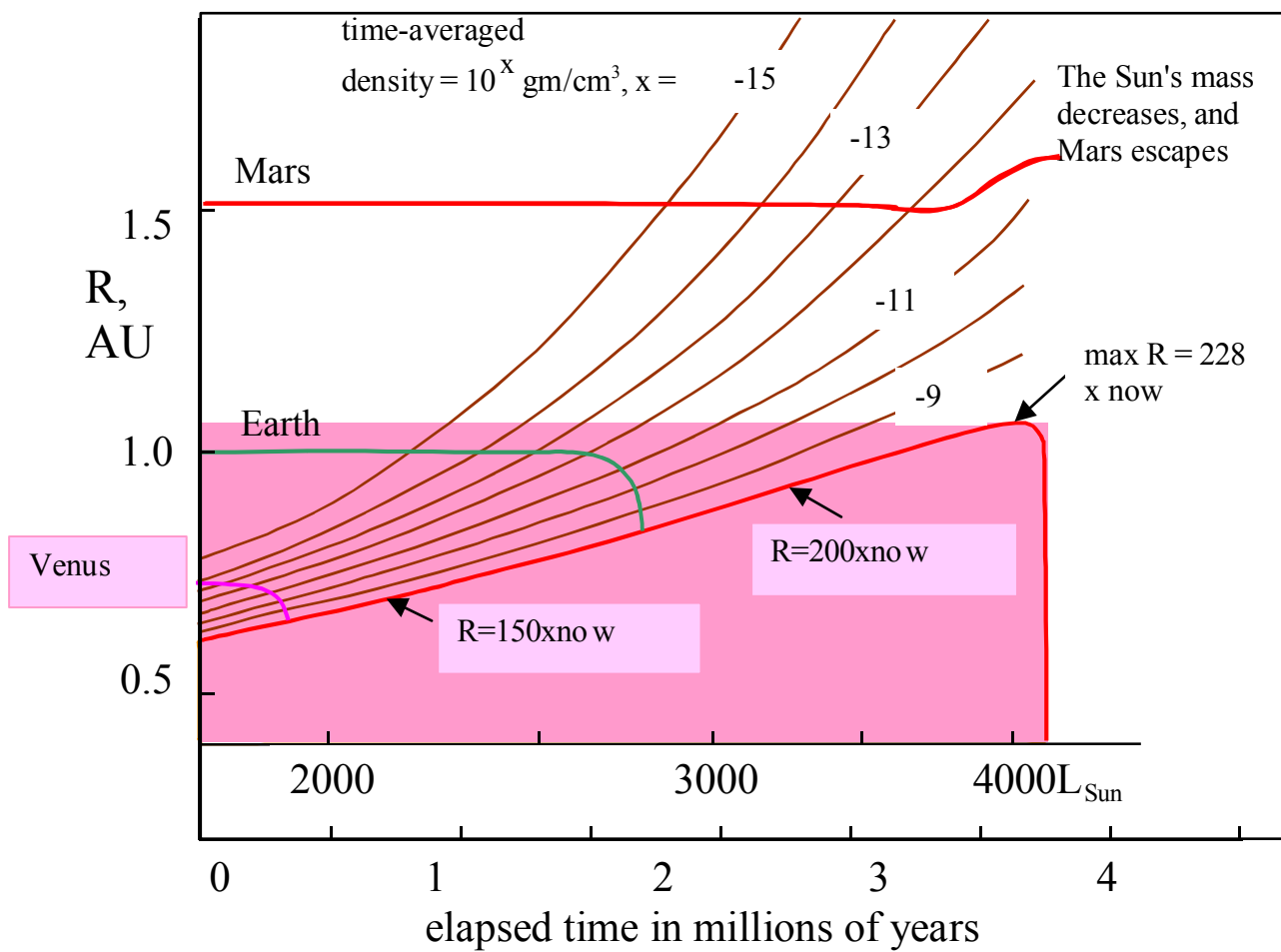


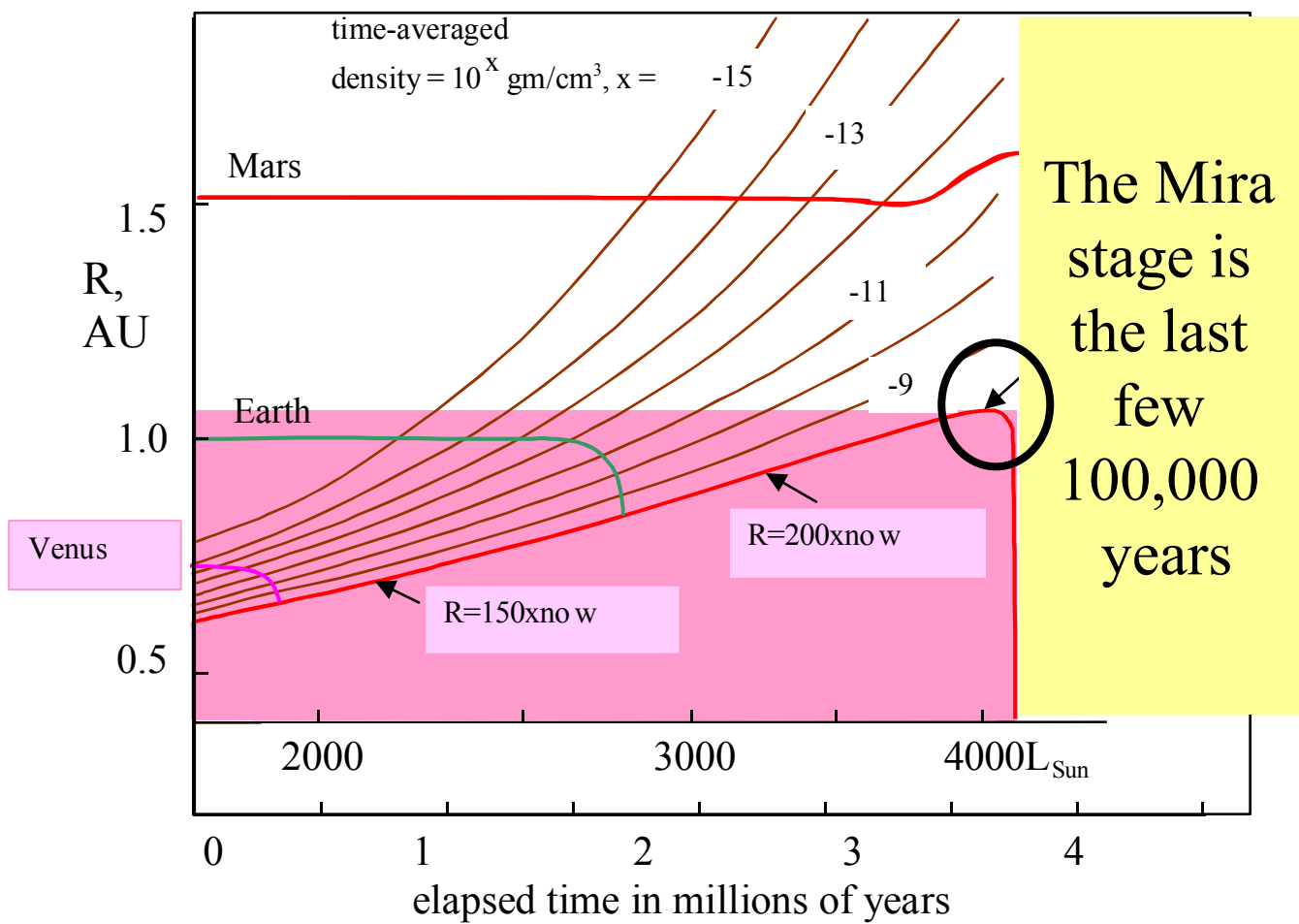


Or perhaps spots with granulation:

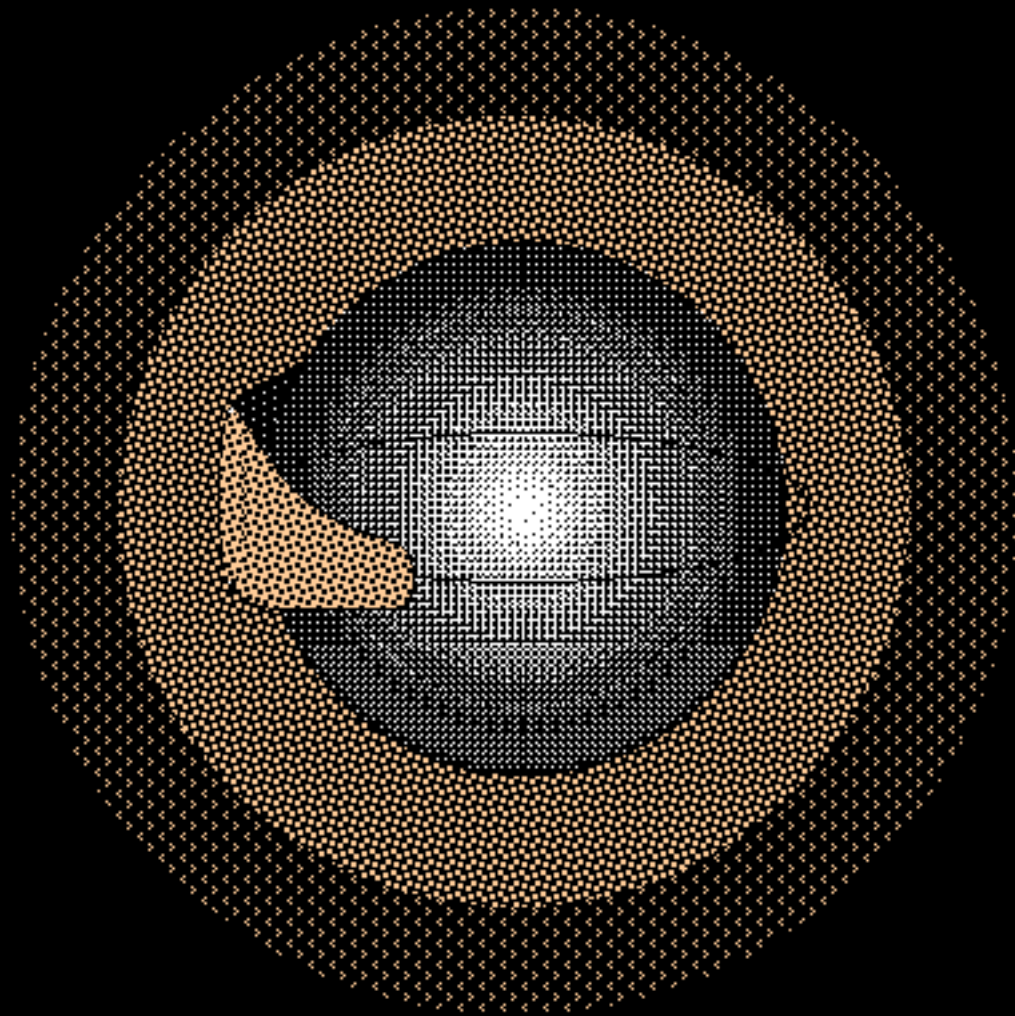


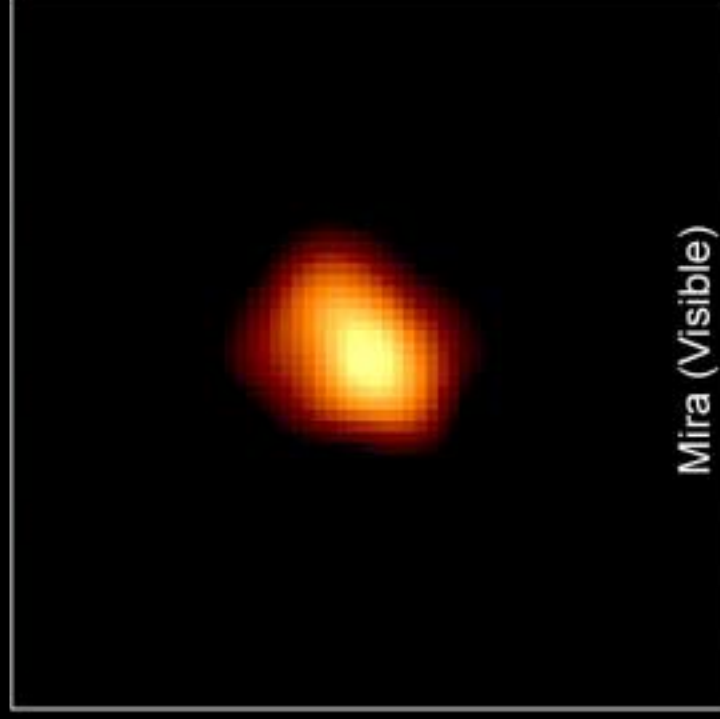




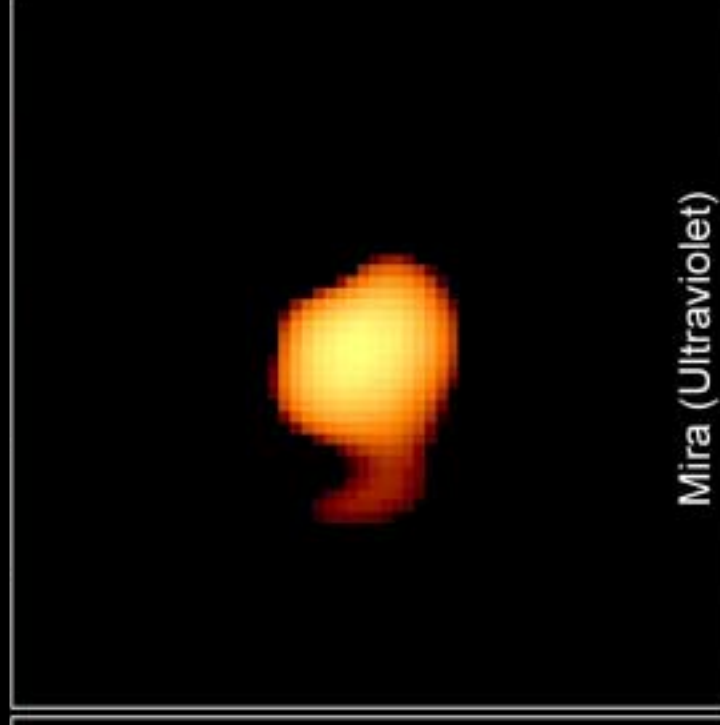


Planets orbiting in Mira winds will produce wakes and shocks; these could give the impression of a non-symmetric or a spotted star.





Mira (Visible)



Mira (Ultraviolet)

## Mira • Omicron Ceti

### Hubble Space Telescope • FOC



PRC97-26 • ST ScI OPO • M. Karovska (Center for Astrophysics) and NASA


# Summary: Departures from spherical symmetry

Nonradial pulsation,  
convection,  
shock instabilities,  
magnetic fields,  
spots,  
companions,  
or the interaction  
of a planet with the  
Mira wind.



How big are these stars, anyway?





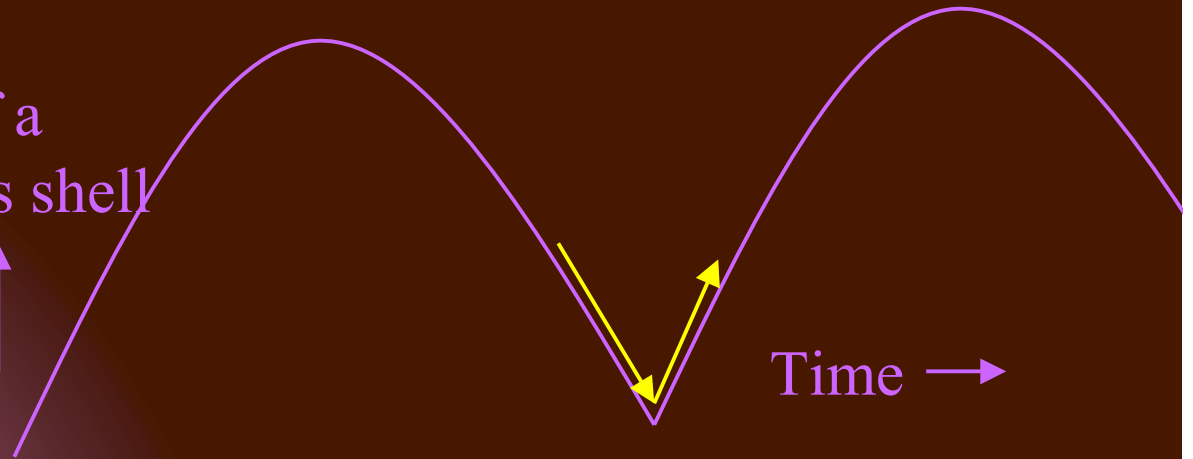
Pulsation models (e.g. Ostlie & Cox):  
F mode  $\Rightarrow$  radii in AU  
approximately equal to pulsation period in days,  
while overtone pulsation would give radii  
about 1.5 to 2 times larger.

Size  $\leftrightarrow$  Mode identification

Dynamical atmosphere models  
 $\Rightarrow$  quite strongly that Miras are  
fundamental mode pulsators,  
 $R \sim 1$  to 2 AU in most cases.

Argument 1: Observed shock amplitudes require higher  $g$  or  $v$ -escape than any overtone pulsators can have.

$R$  of a  
mass shell



Time  $\rightarrow$

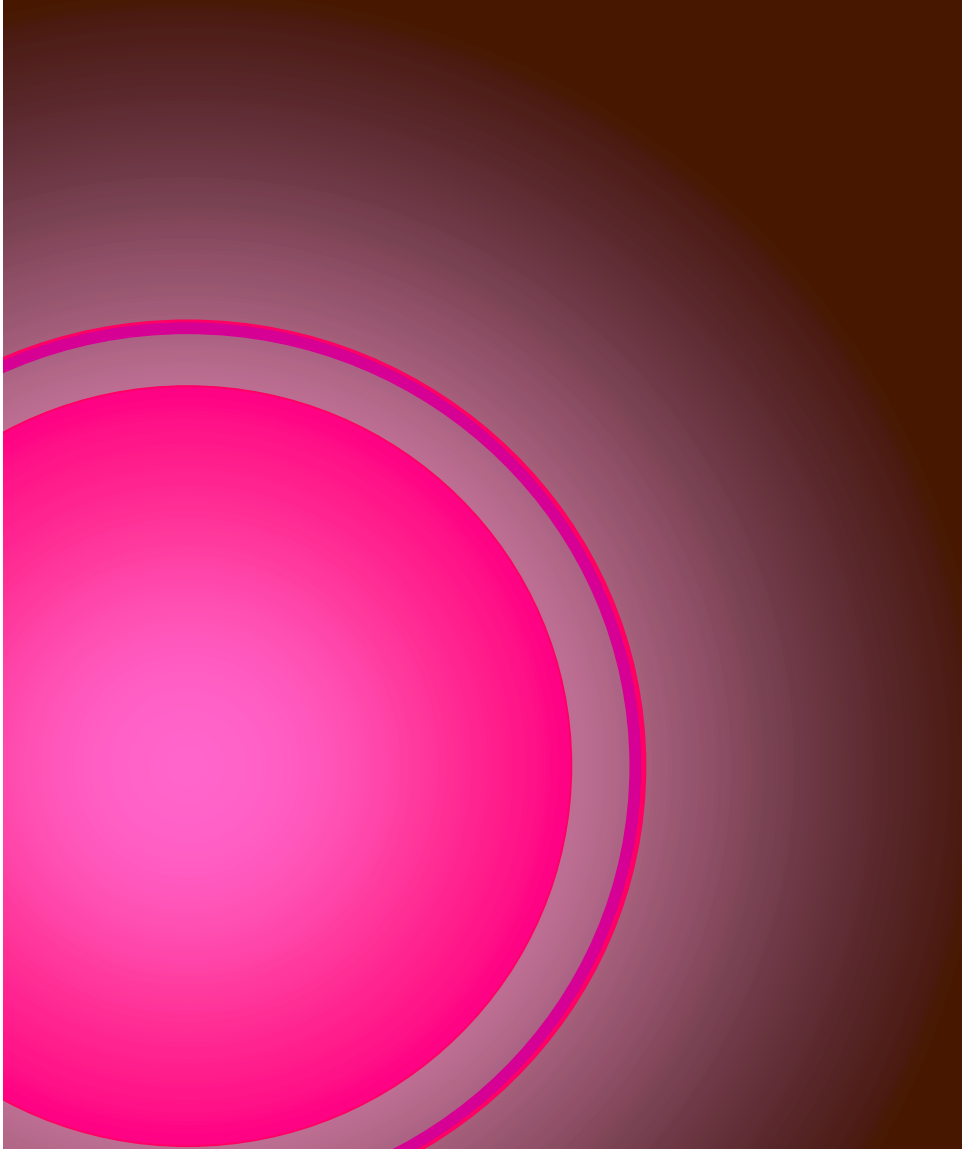
Plane-parallel:  $\Delta v = gP$   
However usually  $\Delta R/R$  is large  
enough to require a slightly  
messier formula.

(Hill & Willson 1979; see  
Willson 2000 ARAA.)



Argument 2: Wave propagation theory:

If  $P < P_{\text{acoustic}}$ , waves propagate with little damping.



Wave propagation theory:

If  $P < P_{\text{acoustic}}$ , waves do not reflect near the photosphere.

Reflection is necessary to get buildup of large amplitudes.



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$$P_{\text{acoustic}} \sim 2\pi H / c_{\text{sound}}$$

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For AGB stars, typically

$$P_{\text{fundamental}} > P_{\text{acoustic}} > P_{\text{overtone}}$$

Therefore, large amplitude overtone pulsation is NOT expected to occur.

Fix  $P$  (the observed quantity) and  $M$  (not free to vary by much and typically showing up in a square root).

Vary  $R$  and/or the driving amplitude to try to get a good model.

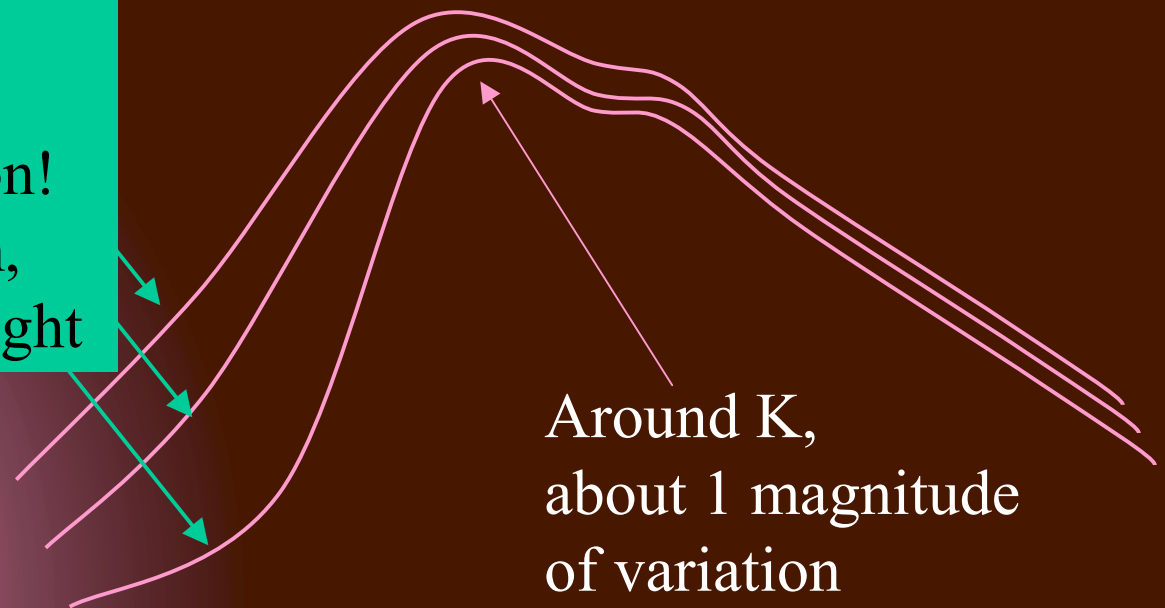
For  $F$  mode models: Easy!

For overtone models:  
Doesn't work! Too much power needed  $\rightarrow$  larger amplitudes and even then the models are very irregular and ill-behaved.

(Bowen 1989 gives details)

# Sketch of Mira SED

In the visible,  
up to 6-7-8-9  
magnitudes of variation!  
There is no continuum,  
even near maximum light



wavelength

# How big? How cool?

Highly probable:

M from 0.8 to 4-5  $M_{\text{sun}}$

But most of them 1-2  $M_{\text{sun}}$

For 1  $M_{\text{sun}}$ ,

Mira L  $\sim 4000 L_{\text{Sun}}$

Mira R  $\sim 200\text{-}250 R_{\text{sun}}$

Effective temperatures

nearly all  $\sim 3000\text{-}3500\text{K}$



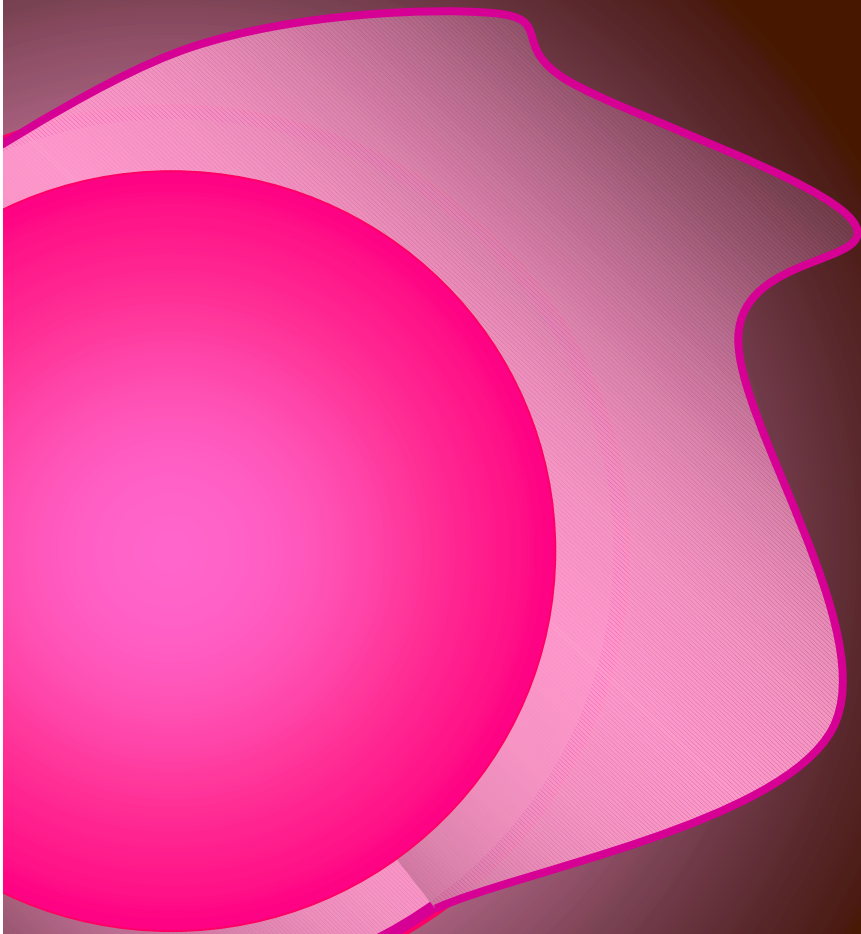


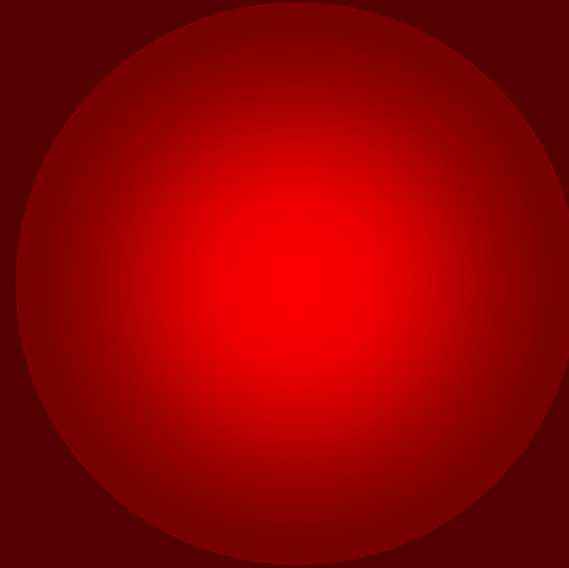
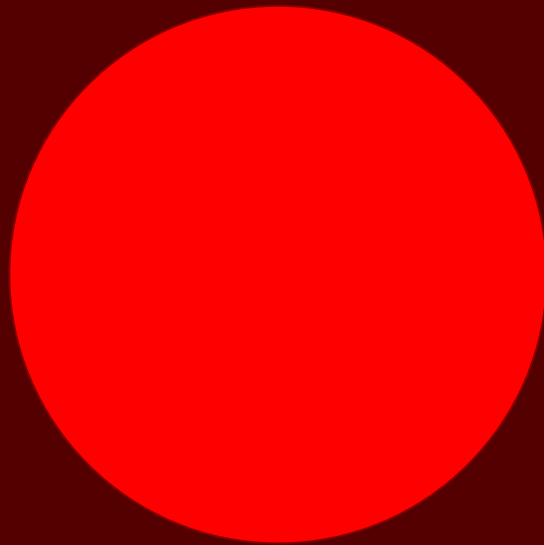
Conclusions: Interesting things to look for in interferometric observations of Miras:

How big is the star?

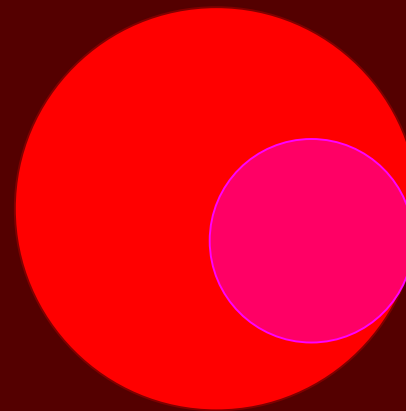
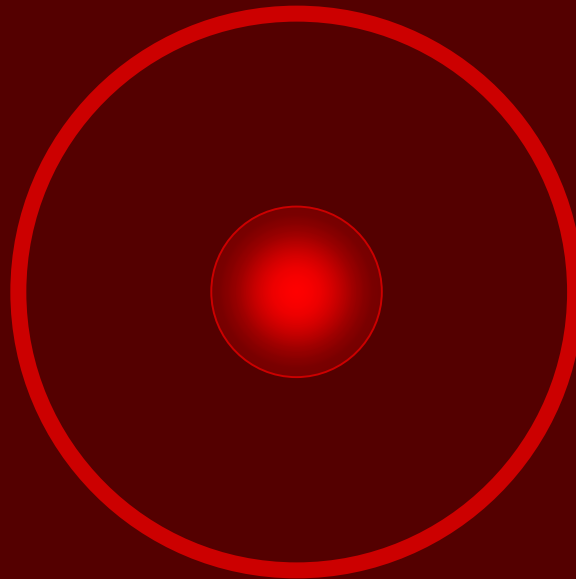
What is the structure of the atmosphere?  
(Shocks, scattering, etc.)

Are there departures from spherical symmetry?





My interpretation of the results of the Perrin et al. paper on R Leo



*The End!*

*(or is it*

***the beginning?)***